ENEE4403 - POWER SYSTEMS

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Department of Electrical and Computer Engineering

Power Systems - General Overview



Traditional electricity delivery system

Power Systems - General Overview



Smart Grids Technology - General Overview



Smart Grids Technology - General Overview

From Conventional Grids to Smart Grids



Source: <u>https://electrical-engineering-portal.com/</u>

References

- Book by: Hussein t. Mouftah and Melike Erol-Kantarci, "Smart Grid: Networking, Data Management, and Business, Models", CRC Press, 2016, Ch. 6: pp. 117-156.
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ECE General Overview

- The energy sector situation in Palestine is highly different compared to other countries in the Middle East due to many reasons: non availability of natural resources, unstable political conditions, financial crisis and high density population.
- Furthermore, Palestine depends on other countries for 100% of its fossil fuel imports and for 87% of its electricity imports.
- In addition high growth of population, increasing living standards and rapid growth of industrial have led to tremendous energy demand in Palestine in recent years.

ECE Palestinian population in 2014 by governorate

Palestine is divided into two geographic areas: West Bank and Gaza Strip. In (2014), according to Palestinian Central Bureau of Statistics (PCBS) the population of Palestine is 4,550,368 in habitants for an area of 6020 km2, being the population density 756 people/km2, distributed as follows: West Bank 494 people/km2 , and Gaza Strip 4822 people/km2, one of the highest population density in the world.

تَجَامَعَهُمُ بِلَكَتِ بِمَالَكُمُ بَعَهُمُ اللَّهُ عَلَيْنَ الْمُعَمَّلُ الْمُعَمَّلُ الْمُعَمَّلُ الْمُعَمَّلُ BIRZEIT UNIVERSITY

ECE Administrative Divisions: Areas A, B and C

- The complex geographical and administrative situation of Palestine can be seen in its administrative divisions made by the Oslo II Accord in 1995, that divided West Bank into three administrative divisions: the Areas A, B and C.
- Area A indicates that full civil and security control belongs to the Palestine. Area B indicates that Palestine has civil control but security control is joint Israel and Palestine. Area C indicates that full civilian and security control is made by Israel.
- Approximately 60% of the land regions in the West Bank are classified as Area C. So, Israel control of these divisions therein severely hinders and affects the potential development of a traditional energy sector's infrastructure and regulations and policies, also hinders development initiatives

ECE Administrative Divisions: Areas A, B and C **BIRZEIT UNIVERSITY**



ECE Administrative Divisions: Areas A, B and C **BIRZEIT UNIVERSITY**





ECE Population density in Palestine



ECE Palestinian population in 2014 by governorate



ECE Average Hours of Electricity Availability per day in summer (2013).





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ECE Average Hours of Electricity Availability per day in Winter (2013).







ECE Energy Consumption

The total energy consumption per habitant in Palestine is the lowest in the region (0.757 MW h/ inhabitant) and costs more than anywhere else in the Middle East countries.





ECE Energy consumption by sectors, 2013.



ECE





Total primary energy consumption in Palestine, 2013.

Distribution of energy consumption for water heating, 2013.

ECE



Electricity distribution (MW h) in Palestine by country in year 2013 (Source: Palestinian Energy and Natural Resources Authority, 2013).

	Israel Electric Company (IEC)	Jordan	Egypt	Gaza Electricity Distribution Co.	Total
West Bank Gaza Strip Palestine (Total)	3,365,597 1,119,211 4,484,808	41,401 0 41,401	0 208,045 208,045	0 402,607 402,607	3,406,998 1,729,863 5,136,861



Electricity residential tariffs in West Bank and Gaza Strip (2014).

Range (kW)	Gaza Strip (\$/kW h)	West Bank (\$/kW h)
1.0–160	0.126	0.151
161–250	0.128	0.159
251–400	0.128	0.179



ECE General Overview West Bank Electrical Network

- The only main transmission lines constructed in the West Bank by IEC are three main 161 kV overhead lines feeding the three main substations: in Hebron, Qalandia (Atarot) and Salfiet (Ara'el).
- The ranges of voltage of West Bank networks are 400V, 6.6 kV, 11kv, 33 kV.

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ECE









Power Losses





Strengths:

- High solar radiation.
- Palestine is geographically situated in an area with very good solar conditions. It has an average of solar irradiation of 5.4 kWh/m2/day.
- Awareness of the Palestinian government about renewable energies.
- Palestine government is in the way to develop the RE law and also creating a wind map.
- Local experience using RE.



- Solar thermal is widely used by around the country. About 70% of hot water is produced by solar thermal technology, which means people already know and rely on RE technology.
- Entrepreneurship character of the private sector.
- Significant potential contribution to cover the future energy demand increase-Electricity energy demand increases yearly for about 6%. RE can help to cover this annual increment.



Drawbacks

- No specific RE regulations defined. Since there are no regulation in the RE market, it is very difficult to create new companies and make investors establish their projects in the country.
- Energy dependency. Palestine depends on the energy imports mostly from Israel.
- Poor infrastructure. Currently the grid in Palestine it is divided into several isolated groups. It's being working for connect the different groups, and so have less points of connection with Israel and more managing capability of the energy in Palestine.



- Small of land surface availability. This is an issue for large scale RE installations. Palestine lacks of terrain, in most of its area it is not possible to build installations or it is needed for agriculture.
- Poor conditions to develop local industry. Due to the lack of energy it is difficult to develop industry.
- Government policy. Government does not have plans to solve the increasing demand of electricity problems neither to solve the short cuts problems.



Thanks For Your Attention

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- There is no electrical power generation in West Bank.
- 96% of electrical energy consumed was imported from IEC.
- The remaining part was imported from Jordan.

 The only main transmission lines constructed in the West Bank by IEC are three main 161 kV overhead lines feeding the three main substations: in Hebron, Qalandia (Atarot) and Salfiet (Ara'el).

- These feeders supply West Bank by 800 MVA, 571 MVA which are supplied to the distribution companies and the remaining 229 MVA is supplied to municipalities.
- West Bank is fed from eight feeders by IEC and two feeders from Jordan.

- The ranges of voltage of West Bank networks are 400V, 6.6 kV, 11kv, 33 kV.
- In Jerusalem Distribution Electric Company (JDECO), the voltage ranges are 400V, 11 kV and 33 kV.
- Northern Electricity Distribution Company (NEDCO) and Southern Electricity Company (SELCO) use 400V, 6.6 kV and 33 kV ranges.

- In Hebron Electric Power Company (HEPCO) the ranges of voltage are 400V, 6.6 kV, 11 kV, 33 kV. Municipalities directly step down the voltage from 33 kV to 400 kV.
- These networks suffer from high transmission and distribution losses (technical and non technical) that varies from 17-32 %.
Overview of Electrical Energy in West Bank

 The maximum capacity of West Bank is nearly 800 MVA. 70% of the supply from Israel comes indirectly through three 161/33 kV substations; one in the south in area C close to Hebron, a second in the north in the Ariel settlement (area C) close to Nablus, and a third in Atarot industrial area (area C) near Jerusalem.

Overview of Electrical Energy in West Bank

- These feeders feed Hebron, Bethlehem, East Jerusalem, Ramallah, Jericho, Salfeet and Nablus.
- 30% comes directly through two 33 kV feeders from Beisan which feed both Jenin and Tubas. And three 22 kV feeders from Ntanya feed both Tulkarm and Qalqiliya . The supply from Jordan comes through 33 kV (can withstand 132 kV) overhead line (20MW) to supply only Jericho.
- The remaining power is generated by decentralized small diesel generators.



Electrical Energy Consumption

- Total energy consumption in 2009 was 2366 GWh.
- The demand for electricity increases at a rate of



Electrical Energy Consumption



Consumption Per Capita

- Electricity consumption in West Bank is about 757 kWh per capita.
- This consumption is considered verv low.



Electric Utilities in West Bank

- The electricity sector in West Bank is fragmented.
- Electricity is distributed by companies and municipalities.
- There are four utilities that distribute electricity in West Bank.

JDECO NEDCO HEPCO SELCO

Electric Utilities in West Bank

- Jerusalem District Electricity Company (JDECO), established in 1928, it is the largest distribution company in the West Bank covers approximately 25% of it. It serves Bethlehem, East Jerusalem, Ramallah and Jericho and connected to Atarot near Jerusalem and area C near to Hebron.
- Northern Electricity Distribution Company (NEDCO), established in 2008 to serve Nablus, Tulkarem, Jenin and other northern regions of the West Bank. But till now only Nabuls and Jenin city are under its responsibility. Connection point is in Areil settlement, at the north of Nablus

Electric Utilities in West Bank

- Southern Electricity Company (SELCO), established in 2002. It serves Dura, Yatta and Dahariah. Connection point is in area C near to Hebron.
- Hebron Electric Power Co. (HEPCO), established in 2000. It serves Hebron and Halhul. Connection point is in area C near to Hebron.
- The remaining areas of the West Bank are under municipal responsibility.



Electricity Customers

- Number of electricity customers in the West Bank is approximately 592940.
- It increases at a rate of 4%.

Electricity Customers in West Bank



Tariff Structure

- The electricity price paid by consumers is somewhat high.
- Uniform tariff does not exist in West Bank.
- Distribution companies control the prices.
- Prices vary from one company to another.

Prepay System



Losses



Load Factor



MVA Capacity



Distribution System in NEDCO & HEPCO



Distribution System in SELCO



Distribution System in JDECO



Transmission Lines

- ACSR transmission lines are used for 33kV,11kV and 6.6kV overhead lines.
- **ABC** transmission lines are used for 0.4kV overhead lines.
- **XLPE** transmission lines are use for 33kv,11kV,6.6kV for underground cables.

Transformers

• Dy11 Step down distribution transformers are used.

High Voltage Transformers	Low Voltage Transformers
15 MVA	1000 kVA
10 MVA	630 kVA
7.5 MVA	500 kVA
5 MVA	400 kVA
3 MVA	250 kVA
2.5 MVA	160 kVA &100 kVA

Example: Nablus Distribution System



Example: Nablus Distribution System

Substation	Capacity (MVA)	Fed from	No. of Transformers (10MVA)
Askar	13	Odala	1
Central	22	Askar	2
Mujeer Aldeen	17	Qussen	2
Wadi Al-tufah	7	Qussen	1

Example: Wadi Altufah S/S

- Single line diagram consists of 59 buses and 25 transformers.
- Transformers are loaded to 40% of rated capacity and 0.92 power factor.



Cont.

• Per unit values for transmission line per phase:

Туре	Voltage	Resistance	Reactance
	(kV)	Pu/ km	Pu/ km
XLPE(120mm ²)	6.6	0.746	0.285
ACSR(95/15)	6.6	0.85	0.641
ACSR(50/8)	6.6	1.515	0.682

Cont.

• Per unit values for transformer per phase:

Capacity	Z _{base}	R(Ω)	Χ(Ω)
(MVA)		Per unit	Per unit
0.25	0.4356	1.579798	0.672635
0.4		1.085859	0.46281
0.63		0.654729	0.277778
1		0.579431	0.247934
10	10.89	0.3434	0.135904

Simulation Results

- The capacity of Wadi Altufah substation is 5.7 MW,
 2.7 Mvar with 0.90 PF.
- A 5.2 MW, 2.4 Mvar is consumed by the load, with
 0.89 PF as an average.
- The losses in the 6.6kV lines is 9%.
- The maximum voltage drop on 6.6 kV was 10.3%.

Example: Bethlehm Distribution System

- Bethlehm is fed from seven 33kV feeders.
- Four main substations.
- The rated capacity is 94.6 MVA.
- Consumed power about 211 GWh.

Substation	Transformers	
	(33/11) kV	
Qobat Rahel	2X15 MVA	
Beit Sahour	10 MVA	
	7.5 MVA	
Jarad	2X10MVA	
Alkhas	5 MVA	
Shufat1	20 MVA	
Shufat2	20 MVA	
Hana	20 MVA	
Efrat	6 MVA	
Jarad	20 MVA	
Sur Baher	8.1 MVA	
Jabae	0.5 MVA	
Total	94.6 MVA	



Example: Alkhas S/S

- Single line diagram consists of 36 buses and 16 transformers.
- Transformers are loaded to 40% of rated capacity and 0.92 power factor.



Simulation Results

- The capacity of Alkhas substation is 1.7 MW, 0.73 Mvar with 0.92 PF.
- A 1.65 MW, 0.7 Mvar is consumed by the load, with
 0.91 PF as an average.
- The losses in the 11kV lines is 3.5%.
- The maximum voltage drop on 11 kV was 4%.

Electrical Energy Problems

- Absence in generating in West Bank.
- Absence of integrated electrical network.
- Lack of supply capacity of electrical energy to meet present and future needs.

Cont.

• Energy prices are very high.

• High transmission and distribution losses.
Future Plans in West Bank

- A project is in its way to be implemented to install four new 161/33 kV transmission substations across West Bank.
- Palestine Energy Transmission Company Ltd. (PETL).
- Connection to seven Arab country grid.

Cont.

- Two new power plants in West Bank will be constructed, which are:
- 1) Jayyus Power Plant in the north, near Qalqiliya.
- Turqumia Power Plant in the south, west of Hebron.

Future Organization of the Power Sector



PEA IEC IPP

45

Palestinian Energy Authority Israeli Electric Corporation Independent Power Producers



Economic Voltage

INCREASING IN VOLTAGE

Cost of conductor material

Cost of insulators Cost of Switchgears

Cost of transformers

Selection of Transmission Lines, Tower Example



Transmission Lines Parameters

» Introduction to transmission Lines (T.L) » Types of Overhead Line Conductors. » Resistance Calculation. » Inductance Calculation. » Capacitance Calculation.

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Overhead transmission System

□ Although underground AC transmission would present a solution to some of environmental and aesthetic (wlz.) problems in overhead transmission lines, there are technical and economic reasons that make the use of underground ac transmission not preferable.

- I The overhead transmission System is mostly used at high voltage level mainly because it is much cheaper Compared to underground system.
- 3) The selection of an economical voltage level for the T.L is based on the amount of power and the distance of transmission.

The economical voltage between Lines in 3¢ is given by 8-

 $V = 5.5 \ v \ 0.62 \ L + \frac{P}{100}$, where

V = Cine Voltage in KV. L = Length al TiL in km. P = Peak real power in KN. Standard fransmission Voltages are established HV (30-230) KV HV (230-765) KV JUHV (765-1500) KV

7 Conducting material Types at overhead line conductors based on » the strength I The material to be chosen for conduction at power should be such that it has the lowest resistance. This would reduce the transmission losses. (a) * (b) 1) Silver resistivity 1.6 Marcm 2) Copper resistivity 1.7 Marcm 3) gold resistivity 2.35 Marcm The weight of material (density) 1) aluminium note: The weight at the aluminium conductor, 2) Copper 3) silver having the same resistivity 4) a luminium resistivity 2.65 uncm 4) gold as that at coppegis Problems & cost, theft, supply is quit limitted roughly 60% less than at copper. 2 In the early days of the transmission of electric power, Conductors where usually copper, but aluminum conductors have completly replaced copper for overhead lines because of the much lower cost and lighter weight of an aluminum conductor compared with a copper Conductor of the same resistance. 3 The most commonly used conductors for high Veltage transmission lines are:-* AAC ALL-Aluminum Conductors All-Aluminum-Alloy Conductors (pinki 151-) * AAAC Aluminum Conductor, Steel-Reinforced (Usi (ine) * ACSR Aluminum Conductor, Alloy-Reinforced. * ACAR * Expanded ACSR > Alumin Steel M ACSR

» Aluminum-alloy conductors have higher tensile strength than the ordinary aluminum. » ACSR consists of a central core of steel strands surrounded by layers of aluminum strands. » ACAR has a central core et higher-strength aluminum surrounded by layers of aluminum. » Expanded ACSR has a filler such as (paper, fiber) separating the inner steel strands from the outer aluminum strands. The filler gives a larger diameter (and hence, lower corona) for a given conductivity and tensile strength. Expanded ACSR is used for some extra-high Voltage Lines. Stranded Conductors » To increase the area stranded conductors are used. This increase the flexibility and the ability of the wire or cable to be bent. » Generally the circular conductors of the same size are used for spiralling. » Each layer at strands is spiraled in the opposite direction at its adjacent layer. This spiraling holds th strands in place (can't open up easily) Stranded Conductors larger sizes) better mech. strength, as well as better handling much more flexible.

Stranded Conductors Aluminium strands steel # at strands strands Total # Istrands -> 1,7,19,37,61,91 Line Resistance: Rac ~ 0 ~ » The de resistance at a solid round conductor at a specific temperature is given by :- $R_{dc} = \frac{f'l}{h} n (*)$ where $P \equiv \text{conductor resistivity at temp T (°C)}$ $l \equiv \text{conductor length (m)}$ $A \equiv \text{conductor cross-sectional area (m²)}$ » Conductor resistance depends on the following factors: I Temperature 2 Spiraling 3 Frequency I Temperature Resistivity if conductor metals varies linearly over normal operating temperatures according to $\rho^{T_2} = \rho^{T_1} \left(\frac{T_2 + T}{T_1 + T} \right)$ ⇒ The conductor resistance increase as temp increases. 7 T = temperatu $\begin{array}{c} \overset{\text{or}}{R_{2}} = R_{1} \left(\frac{T_{2} + T}{T_{1} + T} \right) \\ \overset{\text{T}}{T_{1}} \overset{\text{Kor}}{K_{0}} \left(\frac{T_{1} + T}{T_{1} + T} \right) \end{array}$ constant that d @ For Aluminum on the conductor-material. ⊤≅ 228

2 Spiraling » Since a stranded conductor is spiraled, each strand is longer than the finished conductor. This results in a slightly higher resistance than the value Calculated using equation (*). >> The spiralling increase the resistivity of the conductors to an extent about 2% for the first layer on the centre conductor, about 4% for the second layer, and So on. 3 Frequency "skin effect » When ac flows in a conductor, the current distribution is not uniform over the conductor cross-sectional area and the current density is greatest at the surface of the conductor. This causes the ac resistance to be somewhat higher than the dc resistance. This behavior is known as skin effect. » This uneven destribution does not assume large proportion at 50 HZ up to a thickness of about 10 mm . >> At (50-60) Hz, the ac resistance is about 2 percent higher than the dc resistance. Note:-The ac resistance or effective resistance of a conductor is $R_{ac} = \frac{P_{loss}}{I^2} r$

example A copper cable of 19 strands, each strand 2.032 mm in a diameter is laid over a length of 1km. The temperature rise was found to be 40. Find the value of total R for this cable. third layer = (12 strands) Second luger (6 strands) First layer (1strand) total # at strands = 19 $A_{1s} = \frac{\pi d^2}{4} = \frac{\pi (0.2032)}{4}$ 1 strand For 0 $R_{15} = \frac{PL}{A} = \frac{1.7 \times 10^6 \times 100000}{0.03243}$ = 5.24 r R total = 5.24 = 0.2758 2 I Spiraling effect Firster Ricon = 5.24 Second Rocon = 5.24 = 0.8733 2 Spir. eff, Rocon = 0.8733 × 1.02 - 0.8908 L Vied Rizcon = 5.24 = 0.4367_2 Spir. eff Ryzon = 0.4367*1.04 R = 5.2411 0.8908110.4541 = 0.45412 Rotal = 0.28442 ((3.1% higher when we consider spiraling effect))

remperature effect $R_{2} = R_{1} \left(\frac{T+T_{2}}{T+T_{1}} \right) = 0.2844 \left(\frac{234.5+60}{234.5+20} \right)$ esistance 2) Temperature effect = 0.329 J the resistance at new temp. Compared with (19.3 %) R=0.2758n note: If the cable was carrying a current 200A, the drop from one end to the other end would be about 65.8 volts due to resistance. $\begin{array}{c} 1 = 2 \otimes A \\ (1 = 2 \otimes A \\ 1 = 33 \text{ kv} \\ ((1 = 1 + 2 = 1 + 2 \text{ koltage drop})) \end{array}$ 3 frequency effect At freq 50 Hz the skin depth in a copper is of the order top 10 mm and hence would not have any significant effect as far as this problem is concerned.

Inductance » For Calculating Inductance we need to go to four steps?- □ Magnetic Field Intensity H, from Ampere's Law
 □ Magnetic Flux Density B, (B = M H)
 □ Flux Linkages, (λ)
 □ Inductance From Flux Linkages per ampere. (L=λ/I) B Solid Cylindrical Conductor to de strip Im length A Internal Flux Linkage B External Flux Linkage >> The magnetic field intensity Hx, around a circle of radius X, is constant and tangent to the circle. The Ampere's Law relating Hx to the current Ix is given by? 9 H dl = I enclosed $\left(\begin{array}{c} \mathbf{x} \\ \mathbf{x} \\ \mathbf{y} \\ \mathbf{y} \\ \mathbf{y} \\ \mathbf{x} \\$ > is the Current enclosed at radius X. $H_{x} = \frac{I_{x}}{2\pi x}$

A Internal Inductance » A simple expression can be obtained for the internal flux Linkage by neglecting the skin effect and assuming uniform current density throughout the conductor cross section, i.e. section, i.e. · uniform Current density from (1) $H_{x} = \frac{I_{x}}{2\pi x}$ $H_{x} = \frac{1}{2\pi r^{2}} x$ » For a nonmagnetic conductor with constant permeability Mo, the magnetic flux density is given by: $B_x = M_0 H_x$ $M_0 = permeability$ free space $B_{X} = M_{0} \frac{I}{2\pi r^{2}} X$ = 4 TT * 10° H/1. » The differential flux do for a small region at thickness dx and one meter length at the conductor is $d\phi_x = B_x dx.1$ F dxThe flux do links only the fraction of the conductor from the center to radius X. Thus, on the assumption et uniform Current density, only the fraction $\underline{T}\underline{X}^{*}$ of the total current is linked by the fly \overline{X} , c.e., $d\lambda_{x}=(\overset{x}{\rightarrow})d\phi_{x}$

· B = M IX $d\lambda_{x} = \left(\frac{x}{r}\right) d\phi_{x}$ • $d\varphi = B_x dx$ $=\left(\frac{x^{2}}{r^{2}}\right)\left[-B_{x} dx\right]$ $= \frac{x^{1}}{r^{2}} \xrightarrow{\mu_{0} I \times I} dx$ $d\lambda = \mu_0 I x^3 dx$ » The total flux linkage $\lambda_{int} = \int d\lambda = \frac{\mu_0 I}{2\pi r^4} \int x^3 dx$ = Uo I Wb/m By def, for nonmagnetic material, the inductance L is the ratio of its total magnetic flux linkage to the current I, given by $L = \lambda/I$. The Inductance due to the internal flux linkage is $L_{int} = \frac{\mu_0}{8\pi} = \frac{1}{2} \times 10^7 \text{ H/m}$ Note that Lint is independent at the conductor radius r. B Inductance due to external flux linkage $\oint H_{tan} dl = I_{enclosed}$ $\int^{2\pi x} H_{x} dl = I$ \gg H_x (2 π x) = I $H_x = \frac{I}{2Tx} A/m$ x>r

$$\gg B_{x} = M_{0} H_{x} = 4 \pi \pm 10^{7} \left[\frac{1}{2\pi x}\right]$$

$$= 2 \pm 10^{7} \frac{1}{x}$$

$$d\phi = B_{x} \cdot dx \cdot 1 = 2 \pm 10^{7} \frac{1}{x} dx$$

$$\frac{1}{12\pi x} = \int_{0}^{10} d\lambda = 2 \pm 10^{7} \frac{1}{x} dx$$

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$$\frac{1}{x} = \int_{0}^{10} d\lambda = 2 \pm 10^{7} \frac{1}{x} \ln \frac{1}{2\pi x}$$

$$\frac{1}{x} = \sum \frac{1}{x} \frac{1}{x} \frac{1}{x} \frac{1}{x} \frac{1}{x} \frac{1}{x} \frac{1}{x} \frac{1}{x}$$

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$$\frac{1}{x} = \frac{1}{x} \frac{$$

Composite Conductor :note: $\lambda \rho = 2 \times i \overline{\partial} I \ln \frac{D}{2}$ PIE IY DPI <u></u>GG $I_1 + I_2 + I_3 + \dots + I_N = 0$ $\sum_{i=1}^{N} 1_{i} = 0$ $\lambda_{kPK} = 2 \times 10^7 I_k \ln \frac{D_{PK}}{r'K} + \lambda_{kPK} = 2 \times 10^7 I_k \ln \frac{D_{PL}}{D_{KL}}$ where $D_{kK} = 1^{'K}$ Ly Flux Linkages for the conductor k up to a point p due to the current flowing in conductor k. λ_{Kp}→Flux linkages for the conductor k up to a point p due to the currents flowing in conductors 1, 2, N. $\lambda_{kp} = \lambda_{kp_1} + \lambda_{kp_2} +$ XEN = $2 \pm 10^7 \sum_{j=1}^{7} I_j \ln \frac{D_{Rj}}{D_{kj}}$, where $D_{kk} = r_k^2$ $= 2 \times 10^{7} \sum_{j=1}^{N} I_{j} \ln \frac{1}{D_{kj}} + 2 \times 10^{7} \sum_{j=1}^{N} I_{j} \ln D_{pj}$ $= 2 * 10^{7} \left[\sum_{j=1}^{N} \frac{1}{p_{kj}} + \sum_{j=1}^{N-1} \frac{1}{j \ln p_{j}} + \frac{1}{p_{kj}} \frac{1}{p_{kj}} \frac{1}{p_{kj}} + \frac{1}{p_{kj}} \frac{1}{p_{kj}} \frac{1}{p_{kj}} \frac{1}{p_{kj}} + \frac{1}{p_{kj}} \frac{1}{p_{kj}}$ where $I_{N} = -(I_{1} + I_{2} + \cdots + I_{N-1}) = -\sum_{i=1}^{N-1}$

$$\begin{split} & \mathcal{P}_{k} = 2 \star i\delta^{2} \left[\frac{1}{N} \sum_{n=1}^{M} \ln \frac{1}{D_{kn}} - \frac{1}{M} \sum_{n=1}^{M} \ln \frac{1}{D_{kn}} \right] \\ & \text{Since only the fraction 1 all the total conductor current I} \\ & \text{is linked by this flux, the flux linkage (A) d) subconductor k is} \\ & \lambda_{k} = \frac{0}{N} = 2 \star i\delta^{2} I \left[\frac{1}{N^{2}} \sum_{n=1}^{N} \ln \frac{1}{D_{kn}} - \frac{1}{NM} \sum_{n=1}^{M} \ln \frac{1}{D_{kn}} \right] \\ & \text{The total flux linkage d) conductor x is:} \\ & \lambda_{x} = \sum_{k=1}^{N} \lambda_{k} \\ & = 2 \star i\delta^{2} I \sum_{k=1}^{N} \left[\frac{1}{N^{2}} \sum_{m=1}^{N} \ln \frac{1}{D_{km}} - \frac{1}{NM} \sum_{m=2}^{M} \ln \frac{1}{D_{km}} \right] \\ & = 2 \star i\delta^{2} I \int \frac{1}{N^{2}} \sum_{m=1}^{N} \ln \frac{1}{D_{km}} - \frac{1}{NM} \sum_{m=2}^{M} \ln \frac{1}{D_{km}} \right] \\ & = 2 \star i\delta^{2} I \int \frac{1}{N^{2}} \sum_{m=1}^{N} \ln \frac{1}{D_{km}} - \frac{1}{NM} \sum_{m=2}^{M} \ln \frac{1}{D_{km}} \right] \\ & = 2 \star i\delta^{2} I \ln \frac{1}{N^{2}} \sum_{m=1}^{N} \ln \frac{1}{D_{km}} - \frac{1}{NM} \sum_{m=2}^{M} \ln \frac{1}{D_{km}} \right] \\ & = 2 \star i\delta^{2} I \ln \frac{1}{N^{2}} \sum_{m=1}^{N} \frac{1}{D_{km}} - \frac{1}{NM} \sum_{m=2}^{M} \ln \frac{1}{D_{km}} \right] \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+1} + \ln \frac{1}{n} + \ln \frac{1}{n+\frac{1}{2}}) \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} = \frac{1}{N} \left[\ln \frac{1}{n+\frac{1}{2}} \right] \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ \\ & = \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ \\ & = 1 \ln \frac{1}{(\ln \frac{1}{n+\frac{1}{2}})} \\ \\ & = 1 \ln \frac{1}$$

» if we have Single-phase two-wire line $L_1 = 2 \times 10^7 \ln \frac{D}{r_1} H/m \qquad L_2 = 2 \times 10^7 \ln \frac{D}{r_2} H/m$ $r_1 = 0.7788 r_1$ $r_2 = 0.7788 r_2$ A stranded conductor consists I seven identical Example Strands each strand having a radius r as shown in Figure below, determine the GMR at the conductor interms er. $D_{12} = D_{16} = D_{17} = 2r$ 0.4 = 4r $GMR = \int (O_{11} O_{12} O_{13} O_{14} O_{15} O_{16} O_{17}) (O_{21} O_{22} O_{23} O_{27}) \cdots (O_{71} O_{71})$ $D_{13} = D_{15} = \sqrt{D_{14}^2 - D_{15}^2}$ = 16r2 - 4r2 $= \sqrt{12r^2}$ $= 2\sqrt{3}r$ $= \int (r^{1} \cdot 2r \cdot 2\sqrt{3} r \cdot 4r \cdot 2\sqrt{3} r \cdot 2r \cdot 2r)^{6} (r^{1})(2r)^{6}$ $\int \frac{1}{12} \frac{1}{3} \frac{1}{3} \frac{1}{5} \frac{1}{5} \frac{1}{5}$ = 2.1767 ->> With large number at strands the calculation of GMR can become very tedious. (12, ,) » Usually these are available in the manufacturer's data. (Tables) » The design of a power line requires the value of resistance and reactance to find out the active and reactive power and the voltage drop in the process of power transfer over the transmission line. » Power losses should be limitted to around (5-10) %. A the total power transferred.

		Aluminum			Sieel			Copper Equivalent* Circular	Ultimate	Weight (pounds	Geometric Mean Radius	Approx. Current Carrying	ra Resistance (Ohms per Conductor per Mile)								x _a Inductive Reactance (ohms per conductor per	xa Shunt Capacitive Reactance (megohms per
	Circular				Strand		Outside						25°C (77°F) Small Currents				50°C (122°F) Current Approx. 75% Capacity‡				mile at 1 ft spacing all currents)	per mile at 1 (t spacing)
Code Word	Mils			Diameter (inches)		Diameter (inches)	Diameter (inches)	A W G	Strength (pounds)	mile)	at 60 Hz (feet)	(amps)	dc	25 Hz	50 Hz	60 Hz	dc	25 Hz	50 Hz	60 Hz	60 Hz	60 Hz
Joree Thrasher Kiwi Bluebird Chukar	2 515 000 2 312 000 2 167 000 2 156 000 1 781 000	76 76 72 84 84	4 4 4	0.1819 0.1744 0 1735 0 1602 0 1456	19 19 7 19 19	0.0849 0.0814 0.1157 0.0961 0.0874	1 880 1 802 1 735 1 762 1 602		61 700 57 300 49 800 60 300 51 000		0.0621 0.0595 0.0570 0.0588 0.0534									0.0450 0.0482 0.0511 0.0505 0.0598	0.337 0.342 0.348 0.344 0.355	0.0755 0.0767 0.0778 0.0774 0.0802
Falcon Parrot Piover Martin Pheasant Grackle	1 590 000 1 510 500 1 431 000 1 351 000 1 272 000 1 192 500	54 54 54 54 54 54	3 3 3 3 3 3 3	0.1716 01673 0.1628 01582 01535 0.1486	19 19 19 19 19 19	0.1030 0.1004 0.0977 0.0949 0.0921 0.0892	1.545 1.506 1.465 1.424 1.382 1.338	1 000 000 950 000 900 000 850 000 800 000 750 000	56 000 53 200 50 400 47 600 44 800 43 100	10777 10237 9699 9160 8621 8082	0.0520 0.0507 0.0493 0.0479 0.0465 0.0450	1 380 1 340 1 300 1 250 1 200 1 160	0.0587 0.0618 0.0652 0.0691 0.0734 0.0783	0.0588 0.0619 0.0653 0.0692 0.0735 0.0784	0.0590 0.0621 0.0655 0.0694 0.0737 0.0786	0.0591 0.0622 0.0656 0.0695 0.0738 0.0788	0.0646 0.0680 0.0718 0.0761 0.0808 0.0862	0.0656 0.0690 0.0729 0.0771 0.0819 0.0872	0.0675 0.0710 0.0749 0.0792 0.0840 0.0894	0.0684 0.0720 0.0760 0.0803 0.0851 0.0906	0.359 0.362 0.365 0.369 0.372 0.376	0.0814 0.0821 0.0830 0.0838 0.0847 0.0857
Finch Curlew Cardinal Canary Crane Condor	1 113 000 1 033 500 954 000 900 000 874 500 795 000	54 54 54 54 54 54	3 3 3 3 3 3 3	0.1436 0.1384 0.1329 0.1291 0.1273 0.1214	19 7 7 7 7 7 7	0.0862 0.1384 0.1329 0.1291 0.1273 0.1214	1 293 1 246 1 196 1 162 1 146 1 093	700 000 650 000 566 000 550 000 500 000	40 200 37 100 34 200 32 300 31 400 28 500	7 544 7 019 6 479 6 112 5 940 5 399	0.0435 0.0420 0.0403 0.0391 0.0386 0.0368	1 110 1 060 1 010 970 950 900	0.0839 0.0903 0.0979 0.104 0.107 0.117	0.0840 0.0905 0.0980 0.104 0.107 0.118	0 0842 0.0907 0.0981 0.104 0.107 0.118	0.0844 0.0909 0.0982 0.104 0.108 0.119	0.0924 0.0994 0.1078 0.1145 0.1178 0.1288	0.0935 0.1005 0.1088 0.1155 0.1188 0.1308	0.0957 0.1025 0.1118 0.1175 0.1218 0.1358	0.0969 0.1035 0.1128 0.1185 0.1228 0.1378	0.380 0.385 0.390 0.393 0.395 0.401	0.0867 0.0878 0.0890 0.0898 0.0903 0.0917
Drake Maliard Crow Starling Redwing Flamingo	795 000 795 000 715 500 715 500 715 500 666 600	26 30 54 26 30 54	2 2 3 2 2 2 3	0 1749 0 1628 0 1151 0 1659 0 1544 0 1111	7 19 7 7 19 7	0 1360 0.0977 0 1151 0 1290 0 0926 0 1111	1.108 1.140 1.036 1.051 1.081 1.000	500 000 500 000 450 000 450 000 450 000 419 000	31 200 38 400 26 300 28 100 34 600 24 500	5770 6517 4859 5193 5865 4527	0.0375 0 0393 0 0349 0.0355 0 0372 0 0337	900 910 830 840 840 800	0.117 0.117 0.131 0.131 0.131 0.131 0.140	0.117 0.117 0.131 0.131 0.131 0.140	0.117 0.117 0.131 0.131 0.131 0.131 0.141	0.117 0.117 0.132 0.131 0.131 0.141	0.1288 0.1288 0.1442 0.1442 0.1442 0.1442 0.1541	0.1288 0.1288 0.1452 0.1442 0.1442 0.1471	0.1288 0.1288 0.1472 0.1442 0.1442 0.1491	0.1288 0.1288 0.1482 0.1442 0.1442 0.1442	0.399 0.393 0.407 0.405 0.399 0.412	0.0912 0.0904 0.0932 0.0928 0.0920 0.0943
Rook Grosbeak Égrei Peacock Squab Dove	636 000 636 000 636 000 605 000 605 000 556 500	54 26 30 54 26 26	3 2 2 3 2 2 2	0 1085 0 1564 0 1456 0 1059 0 1525 0 1463	7 7 19 7 7 7	0.1085 0.1216 0.0874 0.1059 0.1186 0.1138	0.977 0.990 1.019 0.953 0.966 0.927	400 000 400 000 400 000 380 500 380 500 350 000	23600 25000 31500 22500 24100 22400	4 319 4 616 5 213 4 109 4 391 4 039	0.0329 0.0335 0.0351 0.0321 0.0327 0.0313	770 780 780 750 760 730	0.147 0.147 0.147 0.154 0.154 0.154	0.147 0.147 0.147 0.155 0.155 0.154 0.168	0.148 0.147 0.147 0.155 0.154 0.168	0.148 0.147 0.147 0.155 0.154 0.168	0.1618 0.1618 0.1618 0.1695 0.1700 0.1849	0.1638 0.1618 0.1618 0.1715 0.1720 0.1859	0.1678 0.1618 0.1618 0.1755 0.1720 0.1859	0.1688 0.1618 0.1618 0.1775 0.1720 0.1859	0.414 0.412 0.406 0.417 0.415 0.420	0.0950 0.0946 0.0937 0.0957 0.0953 0.0953
Eagle Hawk Hen Ibis Laik	556 500 477 000 477 000 397 500 397 500	30 26 30 26 30	2 2 2 2 2 2	0 1362 0 1355 0 1261 0 1236 0 1151	7 7 7 7 7 7	0.1362 0.1054 0.1261 0.0961 0.1151	0.953 0.858 0.883 0.783 0.806	350 000 300 000 300 000 250 000 250 000	27 200 19 430 23 300 16 190 19 980	4 588 3 462 3 933 2 885 3 277	0.0328 0.0290 0.0304 0.0265 0.0278	730 670 670 590 600	0.168 0.196 0.196 0.235 0.235	0.168 0.196 0.196	0.168 0.196 0.196 Same as o	0.168 0.196 0.196	0.1849 0.216 0.216 0.259 0.259	0.1859	0.1859 Same as c	0.1859 Jc	0.415 0.430 0.424 0.441 0.435	0.0957 0.0988 0.0980 0.1015 0.1006
Linnei Onole Ostrich Piper Partridge	336 400 336 400 300 000 300 000 266 800	26 30 26 30 26	2 2 2 2 2 2	0.1138 0.1059 0.1074 0.1000 0.1013	7 7 7 7 7	0 0855 0 1059 0.0835 0.1000 0.0768	0.721 0.741 0.680 0.700 0.642	4/0 4/0 188 700 188 700 3/0	14 050 17 040 12 650 15 430 11 250	2 442 2 774 2 178 2 473 1 936	0.0244 0.0255 0.0230 0.0241 0.0217	530 530 490 500 460	0.278 0.278 0.311 0.311 0.350				0.306 0.306 0.342 0.342 0.345				0.451 0.445 0.458 0.462 0.465	0.1039 0.1032 0.1057 0.1049 0.1074

TABLE A.4 Characteristics of aluminum cable, steel, reinforced (Aluminum Company of America)-ACSR

"Based on copper 97% aluminum 61% conductivity sFor conductor at 75°C, an at 25°C, wind 1.4 miles per nour (2.11/sec). Irequency = 60 Hz : Current Approx. 75% Capacity" is 75% of the "Approx. Current Carrying Capacity in Amps" and is approximately the current which will produce 50°C conductor temp. (25°C rise) with 25°C air temp., wind 1.4 miles per hour.

Example Power is transmitted over the live stranded conductor with series changed over the live stranded conductor with seven strands; each strand 2 mm in diameter. The distance had The distance between the live and neutral wires is 6mm as shown below. Calculate the induction le and reactor contraction reactance at the line in mH per km. GMR = 201767r 2 mm $GMD_{xy} = \int (D_{ia} D_{ib} D_{ic} D_{id} D_{id} D_{ib} D_{ic} D_{id} D_{id} D_{ib} D_{ic} D_{id} D_{id} D_{ib} D_{ic} D_{id} D_{id}$ = 5.99999971 m = 6 m $GMR_{\chi} = GMR_{y} = 2.1767r = (2.1767)(0.001)$ = 0.0021767 $L_{x} = 2 \times 10^{7} \ln \frac{D_{xy}}{D_{xx}} = 2 \times 10^{7} \ln \frac{6}{0.002177} H/m$ = 1.584 × 106 H/m per Conductor L = Lx + Ly = 3.168 * 10° H/m $X_L = WL = 2 TTFL \stackrel{f}{=} Reactance per meter length$ = 2 TT (50) (L) = 2 TT (50) (L)= 9.954 ¥ 10 _2/m = 0,9954 Jr/Km

Notes »The flux Linkage & = L. I » The voltage drop due to this Plux Linkage is $V = ZI = jwLI = jw\lambda$ » When two conductors are placed close to each other, current in one conductor generates the magnetic flux These flux Lines crossing the second conductor due to which a voltage is induced in the second conductor. This process at current en one conductor affecting the other conductor is the mutual inductance. » If we defene the two conductors as 1 and 2, then $M_{12} = \frac{\lambda_{12}}{I_2}$ where O M12 is the mutual inductance between conductor. Land 2. • λ_{12} is the flux Linkage between Conductors 1 and 2. • Iz is the current in conductor 2. Thes en turn introduces the voltage drop in the first conductor which is defended by ? $V_1 = j W M_{12}$

Inductance of 3 PT.L. A Judictance of 3 PT.L. B B Inductance & 30 T.L. a) Symmetrical Spacing (2 puilateral Spacing). b) Asymmetrical Spacing. c) Transposition. d) Bundled Conductor. NK = 2, + 10 ZI Composite Conductor $\lambda_k = 2 \pm 10^7 \sum_{j=1}^{N} I_j \ln \frac{1}{D_{kj}}$ a)) Three phase line with equilateral spacing. ((one meter length)) Assuming Balanced 30 currents:- Ia+ Ib+ Ic=0 => The total flux linkage et phase a conductor is:- $\lambda_a = 2 \star 10^7 \left(I_a \ln \frac{1}{r} + I_b \ln \frac{1}{D} + I_e \ln \frac{1}{D} \right)$ $= 2 \neq i \overline{o}^{7} \left(I_{a} ln \frac{1}{C} + \left(I_{b} + I_{c} \right) ln \frac{1}{D} \right)$ $= 2 \pm 10^{\dagger} (I_a ln \frac{1}{m} - I_a ln \frac{1}{D}) = 2 \pm 10^{\dagger} I_a ln \frac{D}{m}$ $L_{a} = \frac{\lambda_{a}}{L_{a}} = 2 \times \overline{10^{7}} \ln \frac{D}{r} + 1/m = 0.2 \ln \frac{D}{O_{s}} + 1/m + 1/m$ $\lambda_a = \lambda_b = \lambda_c \Rightarrow L_a = L_b = L_c$ solve in GMR This means that the inductance per phase for 30 circuit with equilateral spacing is the same as for one conductor of singly phase circuit.

b)) Asymmetrical Spacing: »Practical transmission lines cannot maintain symmetrical spacing al conductors because al construction considerations. » With asymmetrical spacing, even with balanced currents, the voltage drop due to line inductance will be unbalanced. $\begin{array}{c}
a \\
D_{12} \\
D_{13} \\
D_{23} \\
b
\end{array}$ $\lambda_{a} = 2 \times 10^{7} (I_{a} l_{n} \frac{1}{1} + I_{b} l_{n} \frac{1}{D_{12}} + I_{c} l_{n} \frac{1}{D_{13}})$ $\lambda_{b} = 2 \pm 10^{7} (I_{a} \ln \frac{1}{O_{12}} + I_{b} \ln \frac{1}{m} + I_{c} \ln \frac{1}{O_{23}})$ $\lambda_{c} = 2 \times 10^{7} (I_{a} ln \frac{1}{D_{13}} + I_{b} ln \frac{1}{D_{23}} + I_{c} ln \frac{1}{r_{1}})$ Or sn matrix form $\lambda = LI$ where the symmetrical inductance matrix L is given by: $L = 2 \neq 10^{7} \begin{bmatrix} \ln 1 & \ln 1 & \ln 1 \\ r_{1} & 0_{12} & 0_{13} \\ \ln 1 & \ln 1 & \ln 1 \\ n_{01} & r_{1} & 0_{23} \\ \ln 1 & \ln 1 & \ln 1 \\ 0_{13} & 0_{23} & r_{1} \end{bmatrix}$ ⇒The phase inductances are not equal

c)) Three phase transposed Line: » One way to regain symmetry and obtain per-phase model is consider transposition. » The transposition consists of interchanging the phase configuration every one-third the length. Position 3 c Ь $\lambda_{a_{1}} = 2 \times 10^{7} \left[\frac{1}{a_{1}} \ln \frac{1}{D_{3}} + \frac{1}{b_{1}} \ln \frac{1}{D_{12}} + \frac{1}{c_{1}} \ln \frac{1}{D_{3}} \right]$ $\lambda_{a_{1}} = 2 \times 10^{7} \left[I_{a} \ln \frac{1}{D_{s}} + I_{b} \ln \frac{1}{P_{23}} + I_{c} \ln \frac{1}{P_{n}} \right]$ $\lambda_{a_3} = 2 \neq 10^7 \left[I_a \ln \frac{1}{p_s} + I_b \ln \frac{1}{p_s} + I_c \ln \frac{1}{p_{23}} \right]$ $\lambda_a = \frac{\lambda_{a_1}\left(\frac{1}{3}\right) + \lambda_{a_2}\left(\frac{1}{3}\right) + \lambda_{a_3}\left(\frac{1}{3}\right)}{3} = \frac{\lambda_{a_1} + \lambda_{a_2} + \lambda_{a_3}}{3}$ $= \frac{2 \times 10^{7}}{3} \left[3 I_{a} \ln \frac{1}{D_{5}} + I_{b} \ln \frac{1}{D_{2} 23} + I_{c} \ln \frac{1}{D_{2} 23} \right]$ $= \frac{2 + 10^{7}}{3} \left[3 I_{a} \ln \frac{1}{D_{s}} - I_{a} \ln \frac{1}{D_{12} D_{23} D_{31}} \right]$

 $\lambda_{a} = 2 \neq 10^{7} I_{a} \ln \frac{3}{012} \frac{0}{023} \frac{0}{031}$ $L_{a} = \frac{\lambda \alpha}{T_{a}} = 2 \times 10^{7} \ln \frac{3}{D_{12}} \frac{D_{23}}{D_{31}} \frac{D_{31}}{D_{32}}$ H/m per phase La = 2 + 10 In Deg HIM => This again is at the = 2 * 10 In GMD Ds HIM , Same form as the expression for the induc where $Deg = \sqrt[3]{D_{12} D_{23} D_{31}}$ t'one phase at a single phage Lêne. d)) Bundled Conductor L'êne & shid & stranded solid & stranded d o stranded » Extra-high voltage transmission lines are usually constructed Extra-high Voltage Units Bundling reduces the line reactance, with bundled conductors. Bundling reduces the line reactance, which improves the line performance and increase the power capability at the line. Bundling also reduces the voltage surface gradient, which in turn reduces corona loss, radio interference, and surge impedance. $(\sqrt{\frac{1}{2}})$ » Typically, bundled conductors Consists of two, three, or four subconducters symmetrically arranged in Configuration as shown in Figure above.

» The subconductors within abundle are separated at frequent intervals by spacer-dampers. spacer-dampers prevent clashing, provide damping, and connect the subconductors in parallel. Bundling Reduces Electric Field Increases Effective Strength on Conductor Radius (GMR) Surface Reduces Inductance Reduces Corona GMR = Db GIMR = D GMR = D $= \int (r^2 d d d d J^2)^4$ $= \int (r' \cdot d)^2$ $= \int (r^{1} \cdot d \cdot d)^{3}$ = " r' d2 $= 1.091 \text{V} \text{r}^{1} \text{d}^{3}$ = 2/r'.d C.M. GMR 3 $L_a = 2 \times 10^7 \ln$ H/m

» Three-phase Lines - Parallel Circuits. >> Thre-phase Double-Circuit Lines. A three-phase double-Circuit line consists of two identical 3¢ circuits. The circuits are operated with abc, cba in parallel. Because et geometrical differences between Conductors, Voltage drop due to line inductance will be unbalanced. To achieve balance, each phase conductor must be transposed within it. must be transposed within its group and with respect to parallel 3\$ line. \bullet^{C_2} $a_{|}(\cdot)$ e b2 b O_{α_2} c, \odot The conductor configuration at a completely ample transposed 3-\$ overhead transmission line with bundled conductor is shown below. All the conductors have a radius of 0.74 cm with a 30 cm bundle spacing a)) Determine the inductance per-phase in mH/km and in mH/m. b)) Find the inductive Line reactance per phase in silm at f= 50HZ. 30 cm 30 cm 50 cm 50

Dab = V d13 d14 d2 d24 $= (6 \pm 6.3 \pm 5.7 \pm 6)^{1/4} = 5.9962 m$ Similarly, $D_{bc} = 5.9962 \text{ m}$ Dca = Ud15 d16 d26 $= (12 \neq 12.3 \neq 11.7 \neq 12)^{\frac{1}{4}} = 11.9981 \text{ m}$ The equivalent equilateral spacing between the phases is given by Deg defined as :- $D_{eq} = (D_{ab} \cdot D_{bc} \cdot D_{cq})^{3}$ $= (5.9962 + 5.9962 + 11.9981)^{\frac{1}{3}}$ = 7.5559 m d d $D_{r}^{b} = \sqrt[2]{r'} d$ = (0.7788*r * 30) = 4.1580 Cm a)) Inductance per phase for the given system is :- $L = 2 \neq 10^{7} \ln \frac{Deq}{D_{i}^{b}} + 1 \ln l \text{ phase}$ = 1.04049 + 106 H/m/phase = 1.04049 + 10° mH/m/phase = 1.04049 b)) The inductive line reactance per phase mH/km/phase The inductive unit recurring $f'' = 2\pi fL = 2\pi (56)(1.04049) + 10^6 r/m)$ phase = 3.270 ¥ 104 _1/m/ phase

Transmission Lines Parameters T.L. Capacitance T.L Resistance T.L Inductance Transmission Line Capactance & » Capacitance at transmission Line is the result of the potential difference between the conductors, it causes them to be charged in the same manner as the plates at a capacitor, when there is a potential difference between them the capacitance between conductors is the Charge per unit at the potential difference. 1)) Electric Field and Voltage Calculation 2)) Transmission Line Capacitance for:-[A] Single-Phase Line. B 30 Lines with equal spacing. C 30 Lines, bundled conductor, and unequal spacing. 1)) Grauss's Law -> Electric Field Strength (E) - No Hage between Conductors -- Capacitance C = 2/V Gauss's Law & Total electric flux leaving a closed surface = Total charge within the vollume enclosed by the closed surface. leads to Normal Electric Flux density integrated over the closed surface = charge enclosed

surface integral $\ \ D_1 \ ds = \ \ E_1 \ ds = \ \ \ enclosed$ Where, $\mathcal{E} \stackrel{\text{\tiny def}}{=} \text{permittivity afthe medium} = \mathcal{E}_{r}\mathcal{E}_{o}$ $\mathcal{E}_{o} = \mathcal{B}_{.854} \neq \overline{io}^{20} F/m$ D1 ≜ normal component al electric flux density. EL ≜ normal component efelectric field strength. ds = the differential surface area. Pi Viz Note :-Inside the perfect Conductor, Ohm's clm Law give Ent = 0 That is, the internal's electric field Eint = 0 \$ E E L ds = Qenclosed Im length E E (2) (2) $\Sigma E_{X}(2\pi X)(1) = q(1)$ $E_{x} = \frac{2}{2\pi 5x} \quad V/m$ $V_{12} = \int_{0}^{0_{2}} E_{x} dx = \int_{0}^{0_{2}} \frac{2}{2\pi 5x} dx$ note P2 $V_{12} = \frac{q}{2\pi 2} \ln \frac{D_2}{D_1}$ VIL where, ٤ = ٢, ٢, ÷ P ε. = 8.854 × 10° F/m $V_{12} = \frac{2}{2\pi\epsilon} \ln \frac{D_2}{D} \quad \text{Volts}$

Multi-Conductor System: Conductor k has radius rk and charge 7 ((per meter length of the K conductor)) rk R Pjk Ck Vij J $V_{ijk} = \frac{\mathcal{Z}_k}{2\pi\epsilon} \ln \frac{D_{jk}}{D_{ik}} \quad \text{Volts}$, Ori yottage, thereas $V_{ij} = \sum_{k=1}^{m} \frac{\frac{2}{k}}{2\pi \epsilon} \ln \frac{D_{jk}}{D_{ik}} \quad \text{Volts}$ due all conductors Super-position Theorem Transmission Line Capacitance Single-Phase Line Three-Phase Lines [A] Single-Phase Line $V_{xy} = \frac{1}{2\pi\epsilon} \frac{2 \ln \frac{Dyx}{Dxx}}{2\pi\epsilon} - \frac{2 \ln \frac{Dyy}{Dxy}}{Dxy}$.a cim at clm $= \frac{4}{2\pi 2} \ln \frac{Dy}{Dx} \frac{Dy}{Dxy}$ D H'Y $= \frac{2}{\pi \epsilon} \ln \frac{D}{\sqrt{r_x r_y}}$ due to Symmetry Nolts Vxy $C_{xy} = \frac{\mathcal{X}}{V_{xy}} = \frac{\pi \mathcal{L}}{\ln\left(\frac{D}{\sqrt{\chi}}\right)}$ F/m 000 Notes 000 $\gg V_{21}(q_2) = \frac{q_2}{2\pi s} \ln \frac{D}{r} = -V_{12}$ $\gg V_{12}(q) = \frac{q}{2\pi s} \ln \frac{D}{r}$ $\gg V_{12} = V_{12}(z_1) + V_{12}(z_2)$ $\gg V_{12}(q_1) = \frac{q_2}{2\pi\varsigma} \ln \frac{r}{D}$ ₹2 = - *Ę*

 $C_{xy} = \frac{\pi c}{\ln(\frac{D}{\sqrt{r_x r_y}})}$ if rx = ry $C_{xy} = \frac{\pi z}{\ln(\frac{D}{z})}$ Cxy × y + V_{xy} - $V_{xn} = V_{yn} = \frac{V_{xy}}{2}$ $C_n = C_{x_n} = C_{y_n} = \frac{q}{V_{x_n}} = 2C_{xy} = \frac{2\pi 2}{\ln(\underline{D})}$ $\begin{array}{c} C_{xn} & C_{yn} \\ \bullet & 1 \\ \bullet & 1 \\ x & n \end{array}$ B Three-Phase Line with Equilateral Spacing: $D \qquad D \qquad q_a + q_b + q_c = 0$ $\Rightarrow V_{ab} = \frac{1}{2\pi i} \left[\frac{q}{2a} \ln \frac{D_{b*}}{D_{aa}} + \frac{q}{f_b} \ln \frac{D_{bb}}{D_{ab}} + \frac{q}{f_c} \ln \frac{D_{bc}}{D_{ac}} \right]$ $=\frac{1}{2\pi i}\left[\frac{q_{a}}{2\pi i}\left[\frac{p_{a}}{r}+\frac{p_{a}}{r}\right]\frac{p_{a}}{r}+\frac{q_{b}}{r}\left[\frac{p_{a}}{r}+\frac{q_{b}}{r}\right]\frac{p_{a}}{r}\right]$ $= \frac{1}{2\pi\epsilon} \left[\frac{q_a}{a} \ln \frac{p}{p} + \frac{q_b}{b} \ln \frac{r}{D} \right] + \operatorname{Volts}$ $\Rightarrow V_{ac} = \frac{1}{2\pi \varepsilon} \left[\frac{q}{2a} \ln \frac{D_{ca}}{D_{aa}} + \frac{q}{t_b} \ln \frac{D_{cb}}{D_{ab}} + \frac{q}{t_c} \ln \frac{D_{cc}}{D_{ac}} \right]$ $= \frac{1}{2\pi \varepsilon} \left[\frac{2}{2} \ln \frac{D}{r} + \frac{2}{5} \ln \frac{D}{D} + \frac{2}{5} \ln \frac{r}{D} \right]$ $= \frac{1}{2\pi \xi} \left[\frac{q_a}{ln} \frac{D}{r} + \frac{q_c}{ln} \frac{n}{D} \right]$

 $V_{ab} + V_{ac} = \left(\frac{1}{2\pi\xi}\right) \left[2\frac{q}{2}\ln\frac{p}{r} + \left(\frac{q}{b} + \frac{q}{c}\right)\ln\frac{r}{D}\right]$ $V_{an} = \frac{1}{3} \left(V_{ab} + V_{ac} \right)$ $= \frac{1}{3} \left(\frac{1}{2\pi\varsigma} \right) \left[2q_a \ln \frac{D}{r} + q_a \ln \frac{D}{r} \right]$ $\frac{2a}{2\pi i}$ In D $C_{an} = \frac{2\pi\Sigma}{\ln D}$ F/m (ine to neutral Notes : $V_{ab} = \sqrt{3} V_{an} \left[\frac{+30}{2} = \sqrt{3} V_{an} \left[\frac{\sqrt{3}}{2} + j \frac{1}{2} \right]$ $V_{ac} = -V_{ca} = \sqrt{3} V_{an} \left[\frac{-30}{2} = \sqrt{3} V_{an} \left[\frac{\sqrt{3}}{2} - \frac{1}{2} \right] + \frac{1}{2}$ $V_{ab} + V_{ac} = 3 V_{an}$ 1 $V_{an} = \frac{1}{3}(V_{ab} + V_{ac})$ [] 3\$ with asymmetrical Spacing c Date Date Date Date $C_{an} = \frac{2\pi \epsilon}{\ln(\frac{Deq}{r})}, \quad D_{eq} = \mathcal{J} D_{ab} D_{bc}$ (r) solid (outside diameter) & Avonded
3\$ Bundled Conductor with unequal spacing D D's Ŝ, DAB DBC DAB = GMDAB D_{BC} = GMD_{B,C} DAC = GMD A,C 2 TT 2 C_{an} = In (Deg Db GMR for the bundled D $D_{eq} = \int_{AB}^{3} D_{Bc} D_{Ac}$ 4 conductor $D_{y}^{b} = \sqrt[2]{rd}$ Sub conductor $D_s^b = \sqrt[3]{r} d^2$ Subcond $D_{s}^{b} = 1.091 \sqrt{r} d^{3}$ if the subconductor is strancked outsidec

30 Bundel 10 30 $C_{an} = \frac{2\pi c}{\ln \frac{Deq}{Ob}}$ $C = \frac{2\pi z}{\ln D}$ $C = 2\pi \Sigma$ an In Dee $C = \frac{2\pi 2}{\ln 0}$ 00) DAB NK DECO D D D-Q Dat Dat if stranded conductor exist instead of solid r --- outside diameter A three-phase, 400 kV, 50 Hz, 350 km overhead T.L. has Flat horizontal spacing with three identical conductors. The conductors have an outside diameter of 3.28 cm with 12 m between adjacent conductors. » Determine the capacitive reactance - to-neutral in r/m/phase » Determine the capacitive reactance for the (ine in 1/ phase outside diameter 3.28 cm a = 15.119 m = 3 (12)(24)(12) Deg = V Dab Dac Pbc = 8.163 * 10° MF/m notes Z = 1 2TE In(Deg) Can $Y_n = 2\pi \pm 50 \pm C_n = 2.565 \pm 10^7 - m/m/phase$ Length = 350 km Jphase Yn = 8.978 * 10' 1.1138 × 103 52/phase Reactance = Xn = Yn

Line charging current: The current supplied to the transmission Line capacitance is called charging Current. For a completely transposed For a single-phase circuit operating [3\$ Line that has N = V 10. at line-to-line voltage Vy=Vylo. >> The charging Current is Ichg = Yxy Vxy = jw Cxy Vxy Amp » The phase a charging Currenti Ichg = Van Van = jwan LN >> The capacitor delivers reactive » The reactive power delivered by phase a is power, the reactive power delivered by this line-to-line QCIP = Yan Van = w Cn V w Van Capacitance is $Q = \frac{V_{xy}}{X_{r}} = Y_{xy} V_{xy}^{2}$ >> The total reactive power supplied by the 3¢ line is = w Cxy Vxy var $Q_{C3\phi} = 3Q_{C1\phi} = 3W_{C1}V_{LN}$ $= \sqrt{3}\sqrt{3} \omega Can V_{LN} V_{LN}$ Q_{C3}\$ = W Can V_{LL} Var

Transmission Line Modeling Short Line Model (Less than 80 km) ■ Medium Line Model (80km < L < 250 km) Long Line Model (L>250 km) » Lumped parameter system. » Distributed parameter system. • we use Lumped parameters which give good accuracy for short Lines and for lines at medium length. • If an overhead line is classified as short, shunt capacitance is so small that it can be omitted entirely with little loss at accuracy, and we need to consider only the series resistance R and the series inductance L for the total length of the Line. Short Line Model 8-Z=R+jX VR Load >> line length < 80 km >> Generally MU/LY Lin » Capacitance cab be neglear ted Z = (r + jwL) Cwhere mand L are the per-phase resistance and inductance per = R + j Xunit length, respectively, and L is the line length.

The phase voltage at the sending endis

$$V_{I} = V_{R} + Z I_{R}$$

 $I_{S} = I_{R}$
 $Transmission part
 V_{I}
 $V_{I}$$

Medium Line Model

sokm < Length < 250km.
 As the length of line increases, the line charging current becomes appreciable and the shunt capacitance must be considered.
 For medium length lines, half of the shunt capacitance may be considered to be lumped at each end of the line. This is referred to as the nominal T model and is shown in Figure below :-



Z = total series impedance of the line.<math>Y = botal shunt admittance of the line.<math>Y = (g' + jw c) l

Under normal conditions, the shunt conductance per unit length, while h represents the leakage current over the insulators and due to corona, is negligible and g is assumed to be Zero. C is the line to neutral capacitance per km, and b is the line length.

1.
$$V_{S} = V_{R} + Z I_{L} I_{L}$$

$$= V_{R} + Z (I_{R} + V_{R} \cdot \underline{Y})$$

$$V_{S} = AV_{R} + BI_{R}$$

$$I_{I} = CV_{R} + DI_{R}$$
2.
$$I_{S} = I_{R} + \frac{V_{S} \cdot \underline{Y}}{2} + \frac{V_{S} \cdot \underline{Y}}{2}$$

$$= (I_{R} + V_{R} \cdot \underline{Y}) + \frac{V_{S}}{2}$$

$$I_{S} = I_{R} + \frac{V_{R} \cdot \underline{Y}}{2} + \frac{V_{S} \cdot \underline{Y}}{2}$$

$$I_{S} = Y (1 + \frac{YZ}{2}) V_{R} + (1 + \frac{YZ}{2}) I_{R}$$

$$\begin{bmatrix} V_{S} \\ I_{S} \end{bmatrix} = \begin{bmatrix} (1 + \frac{YZ}{2}) & Z \\ \overline{Y}(1 + \frac{YZ}{2}) & \overline{Y} \end{bmatrix} \begin{bmatrix} V_{R} \\ I_{R} \end{bmatrix}$$

$$A = D = 1 + \frac{YZ}{2} \quad \text{per unit} \quad \text{since five Tr model is a symmetrical two - port networt (A = D)$$

$$C = Y (1 + \frac{YZ}{4}) S$$

.

+



131 Long Line Model 8-

* For the short and medium length Lines reasoning accurate models were obtained by assuming the Line parameters to be Lumped. For lines 250 km and longer and for amore accurate solution the exact effect of the distributed parameters must be considered.



Taking the limit as
$$\Delta x \rightarrow 0$$
, we have

$$\frac{d V(x)}{dx} = z I(x)$$

$$= 0$$

$$\frac{d V(x)}{dx} = z I(x) = 0$$

$$\frac{d V(x)}{dx} = I(x) + y \Delta x V(x + D x)$$

$$\frac{I (x + \Delta x) - I(x)}{\Delta x} = y N(x + D x)$$

$$\frac{I (x + \Delta x) - I(x)}{\Delta x} = y N(x)$$

$$\frac{d I(x)}{dx} = y V(x)$$
and from $0 \Rightarrow$

$$\frac{d I(x)}{dx} = y V(x)$$

を 丁(x) from Q return to 1 - ① M V(x) $\frac{d^2 V(x)}{d^2} = \frac{d I(x)}{d^2}$ substituting $\frac{d T(x)}{dx} = y V(x) \xrightarrow{assec} (x) V(x) = \int (x) v (x)$ return $= \frac{d^2 V(x)}{dx^2} = \frac{z}{dx} \frac{dI(x)}{dx}$ $\frac{d^2 V(x)}{d x^2} = \frac{z y V(x)}{z y^2} \frac{y v_x}{y^2}$ zy= ど, $\frac{d^2 V(x)}{d^2} - \frac{\chi^2 V(x)}{2} = 0$ phase constant $= V(x) = A_1 e^{-x} + A_2 e^{-x}$ attenuation where $\gamma \equiv propagation$ constant = $\sqrt{zy} = x + jB$ $= \sqrt{(r+jwL)(g+jwc)}$ $V(x) = A_1 e^{-\delta x} + A_2 e^{-\delta x}$ $f(x) = \frac{1}{2} \frac{dV(x)}{dx} = from - 0$ $= \frac{\sqrt{2}}{2} \left(A_1 e^{xx} - A_2 e^{xx} \right)$ = V Z (Aie + Aie x) $\frac{1}{Z_c} (A_1 e^{x} - A_2 e^{x}), Z_c = characteristic$ impedance Ze = J Zly F

$$V(x) = A_{1} e^{xx} + A_{2} e^{x}$$

$$T(x) = \frac{1}{2c} (A_{1}e^{x} - A_{2}e^{x})$$

$$T(x) = \frac{1}{2c} (A_{1}e^{x} - A_{2}e^{x})$$

$$A_{1} = ?(1, A_{2} = ?$$

$$\Rightarrow I(x) = \frac{1}{Z_c} \sinh \delta x \, V_R + \cosh \delta x \, I_R$$

Netlate particularly interested in the relation between
the sending end and the receiving end of the line.
Setting
$$x = l$$

 $V(l) = V_3$
 $I(l) = I_3$
 $\Rightarrow V = \cosh \delta l V_R + Z_c \sinh \delta l I_R$
 $I_3 = \frac{1}{2c} \sinh \delta l V_R + \cosh \delta l I_R$
 $\begin{bmatrix} V_1 \\ I_3 \end{bmatrix} = \begin{bmatrix} C_{01h} \delta l \\ Z_c \sinh \delta l \\ C_{0h} \delta l \end{bmatrix} \begin{bmatrix} V_R \\ I_R \\ I_R \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} (+ \frac{V2}{2}) & 2 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} (+ \frac{V2}{2}) & 2 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} (+ \frac{V2}{2}) & 2 \\ V_1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} (+ \frac{V2}{2}) & 2 \\ V_1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} (+ \frac{V2}{2}) & 2 \\ V_1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} V_1 \\ V_1 \\ V_2 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$

$$O = Z' = Z_{c} \sinh \delta U$$

$$= \int \overline{Z} \int \sin h \delta U$$

$$= Z \int \frac{\sinh \delta U}{\sqrt{2y'}U} = Z \frac{\sinh \delta U}{\gamma U}$$

$$(\sinh \delta U = 1 + \frac{Z' \gamma'}{2}$$

$$(\cosh \delta U = 1 + \frac{(Z_{c} \sinh \delta U \gamma)}{2} = 1 + \frac{Z_{c} \sinh \delta U}{2} + \frac{2}{2} = \cosh \delta$$

$$\frac{Y'}{2} = \frac{1}{Z_{c}} + \frac{(\cosh \gamma U - 1)}{\sinh \gamma U} = \tanh \frac{\delta U}{2}$$

$$= \frac{1}{Z_{c}} - \frac{(\cosh h \gamma U - 1)}{\sinh \gamma U} = \tanh \frac{\delta U}{2}$$

$$= \frac{1}{Z_{c}} - \tanh \frac{\delta U}{2}$$

$$= \frac{1}{Z_{c}} - \frac{\cosh h (\delta U/2)}{\delta U/2}$$

$$Z_{c} = \sqrt{2U}$$

 $\frac{\text{Notes-}}{\text{cosh}(\chi_l)} = \cosh(\chi_l) \cdot \cos(\beta_l) + j \sinh(\chi_l) \cdot \sin(\beta_l)$ $\sinh(\chi_l) = \sinh(\chi_l) \cdot \cos(\beta_l) + j \cosh(\chi_l) \cdot \sin(\beta_l)$

Lices Less Line :

$$Z = jwL - a.la.$$
 (r=o)
 $y = jwC - S/m$ ($g=o$)
 $Z_{3} = \sqrt{\frac{1}{3}} = \sqrt{\frac{1}{3}wL} = \sqrt{\frac{1}{2}} = \frac{1}{2}$ surge Impedance
purely resistive.
 $Y = JZy = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = jw\sqrt{LC} = j\beta m^{1}$
 $Z = \sqrt{Z}y = \sqrt{(jwl)(jwc)} = 2m^{1}$
 $Z = \sqrt{(jwc)} =$

IT-model for Loss-less line)

$$\frac{\text{model}}{2} \stackrel{\text{s}}{=} \frac{1}{2c} \sinh \delta U$$

$$= j \frac{Zc}{2c} \sin (\beta U)$$

$$= j \frac{Zc}{2} \frac{Sin (\beta U)}{SU/2} = \frac{Y}{2} \frac{4anh (j \beta U)}{j \beta U/2}$$

$$= \frac{Y}{2} \frac{Sinh (j \beta U)}{(j \beta U)}$$

$$= \frac{Y}{2} \frac{Sinh (j \beta U)}{(j \beta U)} \cosh (\frac{j\beta U}{2})$$

$$= (\frac{j w CU}{2}) \frac{j (Sin (\beta U))}{(j \beta U)}$$

$$= \frac{j w CU}{2} \frac{4an (\beta U)}{\beta U}$$

$$= \frac{j w CU}{2}$$

$$= \frac{j w CU}{2}$$

$$TT = Equivalent Circuit ((Leos Less Line)) \stackrel{\text{d}}{=}$$

$$\frac{V}{2} \frac{V}{2} \frac{V}{2} \frac{V}{2} \frac{V}{2} \frac{V}{2}$$

$$= (j w LU) (\frac{Sin\beta U}{\beta U}) = j \chi^{2} R$$

$$\frac{V}{2} = (j w LU) (\frac{Sin\beta U}{\beta U}) = j w CU S$$

(1)

11

For a lossless line :- $V(x) = A(x) V_R + B(x) I_R$ $= \frac{J Sin(Bx)}{Z_c} V_R + \frac{C_0}{B_x} (B_x) I_R$

Wave Length ((Loss Less Line))
$$\stackrel{\circ}{=} A$$
 wavelength is the disface regard
to change the phase of the Jolley
 $V = \frac{W}{B} = \frac{2\pi}{B}$
 $\lambda = \frac{2\pi}{B} = \frac{2\pi}{WLC} = \frac{1}{FVLC}$
 $The expression for the inductance per unit length L and
copacitomic per unit length C aD a transmission line were
derived in previous chapter. When the internal flux linkage
of a conductor is neglected GMRL = GMRC
 $\lambda = \frac{1}{F\sqrt{Ho}E_v}$
 $Mo = 4\pi \pm 10^7$ $\implies \lambda = 6000 \text{ km}$, for 50 Hz
 $E_v = 8.85 \pm 10^2$
 $\implies F\lambda = v = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{Ho}E_v}$
 $= Velocity$ aD propagation aD
Nothinge and current waves on
 $loss-less Line$
 $\neq V(x) = R(x)V_R + B(x)T_R$
 $\neq I(s) = C(x)V_R + D(x)T_R$
 $= \frac{1}{V_{LC}} V_R + Cos(Px)T_R$$

Vialed Ze =
$$\sqrt{L/C}$$
 SIL = $\sqrt{r_{etabl}/Z_{e}}$
(Kv)
230 380 140
345 285 420
500 250 1000
765 257 2280
No Theore Profiles:
Nu (x) = [cos(px)] VANL
Var (x) = Ze Singsr IRAC
Vial
Var (x) = Ze Singsr IRAC
Vial
Var (x) = $\sqrt{L(x)} = \sqrt{L(x)} + \sqrt{L(x)} = (\sqrt{L(x)}) + \sqrt{L(x)} + \sqrt{$

$$\frac{5}{18} + \frac{5}{18} + \frac{5}{18}$$

$$\frac{In + enrms + SIL}{P = \frac{V_R V_s}{\chi^3} \sin \delta} = \frac{V_R V_s}{\chi^3} \sin \delta}{\chi^3} = \frac{V_R V_s}{\chi^3} \sin \delta} = \frac{V_S V_R \sin \delta}{Z_c \sin \beta L}$$

$$= \frac{V_S V_R \sin \delta}{Z_c \sin \beta L} = \frac{V_S V_R}{Z_c} \cdot \frac{Sin \delta}{Sin(2\frac{\pi L}{\lambda})}$$

$$= \left(\frac{V_S V_R}{V_{rated}}\right) \cdot \frac{Sin \delta}{Z_c} + \frac{Sin \delta}{Sin(2\frac{\pi L}{\lambda})}$$

$$= \left(\frac{V_S v_R}{V_{rated}}\right) \left(\frac{V_R}{V_{rated}}\right) \cdot \left(\frac{V_{rated}^2}{Z_c}\right) \cdot \frac{Sin \delta}{Sin(\frac{2\pi L}{\lambda})}$$

$$= \left(\frac{V_S v_R}{V_{rated}}\right) \left(\frac{V_{R} v_R}{V_{rated}}\right) \left(\frac{SIL}{\lambda}\right) \cdot \frac{Sin \delta}{Sin(\frac{2\pi L}{\lambda})}$$

(

ngx =	Sin (2 TT 6)	Voltage	SIL	Typical Thermal Rating (MW)
	$\left(\frac{1}{\lambda}\right)$	230	150	400
A	()	345	400	1200
12 - 1 - 1	([], [max])	500	900	2600

Maximum Power Flow (Lossy Line)⁵

$$A = (osh(81) = A l \theta_A$$

$$B = \overline{Z} = \overline{Z} l \theta_{\overline{A}}$$

$$I_{R} = \frac{V_{S} - A V_{R}}{B} = \frac{V_{S} \frac{\dot{e}^{S}}{Z} - A V_{R} \frac{\dot{e}^{9}}{R}}{\overline{Z} \frac{\dot{e}^{9}}{E}}$$

$$S_{R} = P_{R} + j \theta_{R} = V_{R}^{*} I_{R}^{*} = V_{R} \left[\frac{V_{S} e^{-} - A V_{R} e^{-}}{\overline{Z}} \right]^{*}$$

$$= \frac{V_{R} V_{J}}{\overline{Z}} \frac{\dot{e}^{(\theta_{Z} - \delta)}}{E} - \frac{A V_{R}}{\overline{Z}} \frac{\dot{e}^{j(\theta_{A} - \theta_{Z})}}{E} \right]^{*}$$

$$P_{R} = Re(S_{R}) = \frac{V_{R} V_{S}}{Z} \cos(\theta_{Z} - \delta) - \frac{A V_{R}}{\overline{Z}} \frac{\dot{e}^{j(\theta_{Z} - \theta_{R})}}{E}$$

$$F_{R} = Re(S_{R}) = \frac{V_{R} V_{S}}{Z} \cos(\theta_{Z} - \delta) - \frac{A V_{R}}{\overline{Z}} \frac{\dot{e}^{j(\theta_{Z} - \theta_{R})}}{E}$$

$$F_{R} = Re(S_{R}) = \frac{V_{R} V_{S}}{Z} \cos(\theta_{Z} - \delta) - \frac{A V_{R}}{\overline{Z}} \frac{\dot{e}^{j(\theta_{Z} - \theta_{R})}}{E}$$

 P_{max} $Q_z = S$

$$\frac{Varson (3510m L.ine Steady State Operation & Without we talk about 40.550 co
Signal (310m Line Steady State Operation & Tile what we really mean plan
Signal (310m Line Steady State Operation & Tile what we really mean plan
For the converting Statem and Load
Shalow Due power System
(1) reduce the Transit
The box power System
(1) reduce the Transit
(1)
Power Plan on transmission Line (2)
Muse has not and clip power through
(1) The set of the set of the set
(1) reduce the Transit
(1) reduce$$

$$P_{r} = \frac{|v_{s}||v_{r}|}{|z|} \cos (\theta - \delta) - \frac{|v_{r}|^{2}}{|z|} \cos \theta$$

$$P_{r} = \frac{|v_{s}||v_{r}|}{|z|} \cos (\theta - \delta) - \frac{|v_{r}|^{2}}{|z|} \cos \theta$$

$$P_{r} = \frac{|v_{s}||v_{r}|}{|z|} \sin (\theta - \delta) - \frac{|v_{r}|^{2}}{|z|} \sin \theta$$

$$P_{r} = \frac{|v_{s}||v_{r}|}{|z|} \sin (\theta - \delta) - \frac{|v_{r}|^{2}}{|z|} \sin \theta$$

$$P_{s} = \frac{|v_{s}||v_{r}|}{|z|} \cos \theta - \frac{|v_{s}||v_{r}|}{|z|} \cos (\theta + \delta)$$

$$P_{s} = \frac{|v_{s}|^{2}}{|z|} \sin \theta - \frac{|v_{s}||v_{r}|}{|z|} \sin (\theta + \delta)$$

Pr =
$$|V_{3}||V_{1}|$$
 sin 8
Qr = $|V_{3}||V_{1}|$ cos 8 - $\frac{|V_{1}|^{2}}{X}$
As 8 is normally small; cos 8 ≈ 1
Qr = $|V_{3}||V_{1}|$ _ $|V_{1}|^{2}$
Qr = $|V_{3}||V_{1}|^{2}$ ($|V_{3}| - |V_{1}|$)
 $|V_{1}|^{2}$

1. For fixed values it Vi, Vr and X the real power depending on angle & the phase angle by which is leads ir. This angle S is called power angle. When S = 90 P is maximum, For system stability (considerations & has to be kept well below 90°. Just vij e list range (20-3°) 14 T.L. vije isto avi e live distarbances will 90° 2. Power Can be transferred over line even when [Vs] 5[Vr]. The phase difference & between Vr and Vs causes the flow at power in the line. Power systems are operated with almost the same voltage magnitudes (i.e., 1pm) At important busses by using methods at Voltage (Control. becare this provides a much better operating conditions for the system 3. The maximum real power transferred over a line increases with increase in its and Vr, An increase of 100% in Vr and Vs increases the power ing transfer to 400%. This is the reason for adopting high and extra high transmission voltages . cius k (into se and picture)

4. The maximum real power depends on the reactance X which is directly proportional to line inductance. A decrease in inductance increases the line Capacity. The line inductance can be decreased by using bundled conductors.

The series with the line. This method is known as series compensation. The series capacitors are usually installed at the middle of the line: (Positive Reactance + negative Reactance) - effective Reactance + negative 5. The reactive power transferred over a line is directly proportional to (IVII-IVII) c.e., voltage drop along the line and is independent et power angle. This means the voltage drop on the Line is due to the transfer of reactive power over the line. To maintain agood voltage profile, reactive power control is necessary.

Voltage Control

Reactive Power compensation equipment has the following effects: 1. Reduction in current: $S = P + jQ = Q+, S+ = Ib_{V} = count V_{S, VT}$ 2. Mainteiner Voltage profile within limits. 3. Reduction al losses in the system Q'RHS side It 4. Reduction in investment in the system per KW al load supplied. 5. Decrease in KVA loading of generators and lines. This decrease in KVA loading relieves overload condition or releases capacity For additional load growth. 6. Improvement in power factor of generators. Reactive compensation of I.L. Totatic Var Compensation. Totating Compensators (synchronous compensator) Using Transformer. (Tap transformer) Power Electronica (STAT Com) Static Compensation

The performance of transmission lines, especially those of medium length and longer, can be improved by reactive compensation adaseries or parallel type.

Deries Compensation consists at a capacitor bank placed in series with each phase conductor at the Line. Series Compensation reduces the series impedance at the Line, which is the principal cause of voltage drop and the most important factor in determining the maximum power which the Line can transmit.

I Shunt compensation repers to:

The placement of inductors from each line to neutral to reduce partially or completely the shunt susceptance of a high-voltage line. which is particularly important at light loads when the voltage at the receiving end may otherwise become very high. ((Shunt Reactors))
Shunt Capacitors are used for lagging Prover factor circuits created by heavy loads. The effect is to supply the requisite reactive power to maintain the receiving end very high eact is factory level.

A 50 Hz, 138 KV, & phase transmission line is 200 km
The distributed line parameters are
R = 0.1 -21 km
L = 1.2 mH1km
C = 0.01 MF1km
G = 0
The transmission line delivers 40 MW at 132 KV with
0.95 power factor legging . Find the sending end voltage
and current, and also the transmission line efficiency.
Solution: For the fiven values D R,L and C, we have for w = 217(50),
Z = 0.1 + j 0.377 = 0.39 [75:14° n/km.
y = j3.14 × 10⁵ = 3.14 × 10⁵ [90 - 07/km.
From the above values
Z =
$$\sqrt{(21y)}$$
 = 352.42 [-7.43° n
 $V_1 = \sqrt{205100} L_2^2$ = 0.2213 [82.57° = 0.0286 + j 0.2194
 $V_2 = 2007zy = 0.2213 [82.57° = 0.0286 + j 0.2194$
 $V_1 = 2007zy = 0.2213 [82.57° = 0.0286 + j 0.2194$
 $V_2 = \sqrt{100} L_2 = \frac{8^2 + e^2}{2} = 0.975 [0.37°$
The values of power and voltage specified in the problem
refers to 3-phase and line to line quantities.
 $V_2 = 76.2 L_0^2 = kV$
diso, using V2 as reference; $M_2 = 0^2$, we get
 $V_2 = 76.2 L_0^2 = kV$

Now per phase power supplied to the load. $P_{ioad} = \frac{40}{3} = 13.33$ MW. Given the value I power factor = a. 95, we can find I2 Pload = 0.95 | V2 | . | I2 | Thus, |I21 = 184.1 Also, since Iz lags V2 by Cos 0.95 = 18.195, $I_2 = 184.1 [-18.195]$ tinally, we have :-V1 = V2 coshol + Zc I2 sinhol Sending end voltage. V1 = 82.96 / 8.6 KV J Voltage at the 30 sendingend. Similarly, $I_{I} = I_{2} (osh \& l + \left(\frac{V_{2}}{Z_{c}}\right) sinh \& l$ Sending end current. 5 \$79.46 L17.79 (Pover) Ps We now calculate the efficiency at transmission. Perphase input power, Pin = Re (V, I,) = 14. 69 MW Hence, $\gamma = \frac{13.33}{11.69} = 0.907.$ That is, the efficiency of transmission is 90.7%.

A 3 phase 132 KV overhead line delivers 60 MVA at 132KV and power factor 0.8 lagging at its receiving end. The constants at the line are A = 0.98 13° and B=100 175° ohmsper phase, Find (a) sending end voltage and power angle. (b) sending end active and reactive power. (c) line losses and vars absorbed by the line. (d) and (e) Solution :-] b vin (phase voltage) $\frac{1}{\sqrt{(a)}} = \frac{132000}{\sqrt{3}} = 76210 \sqrt{2}$ JAK $I_{r} = \left[\frac{60 \times 10}{3}\right] \left[\frac{132000}{\sqrt{3}}\right]$ $S_r = V_r I_r^*$ $I_r = 2.62.43/-36.87^{\circ}$ - $cos^{\circ}p.F$ $V_s = A \cdot V_P + B \cdot I_r$ = (0.98 <u>l</u>3)(76210 <u>l</u>0) + (100 <u>l75</u>)(262.43 <u>l-36.87</u>)= 97.33 × 10 (11.92° V Sending end Line voltage = (V3) (97.33) KV = 168.58 * Power angle (S) = 11.92° (d) capacity at static compensation equipment at the receiving end to reduce the sending end voltroge to 145 KV for the same load conditions. (a) vs I (we need to = 145 KV minute 132 kV reduce) (e) The unity power factor load which can be supplied Logd at the receivingend with 132 KV as the line Voltage at both the ends. 132KV 132K purely resistive load. (26) -> P.f.

(a)
$$P_{r} = 60 \times 0.8 = 48 \text{ MW}$$

 $|v_{r}| = 145 \text{ KV}$
 $|v_{r}| = 132 \text{ KV}$
 $|v_{r}| = 132 \text{ KV}$
 $|v_{R} = |v_{S}||v_{r}||B|^{2} \cos(B-S) - 1814W_{r}|^{2}|B|^{2} \cos(B-S)$
 $|v_{R} = 191.4 \cos(B-S) - 170.75 \cos(72)$
 $(so(B-S) = 0.5275$
 $|B-S| = 0.5275$
 $|B-S| = (c^{2}s'(0.5275)) = 58.16^{\circ}$
 $|C-S| = (c^{2}s'(0.5275)) = 58.16^{\circ}$
 $|C-S| = (v_{S}||v_{r}||B|^{2} \sin(B-S) - 181|v_{r}|^{2}|B|^{2} \sin(B-S)$
 $= (v_{S}||v_{r}||B|^{2} \sin(B-S) - 181|v_{r}|^{2}|B|^{2} \sin(B-S)$
 $= (v_{S}||v_{r}||B|^{2} \sin(B-S) - 181|v_{r}|^{2}|B|^{2} \sin(B-S)$
 $= (62.60 - 162.40)$
 $= v_{res} Irms Irms In(B-S)$
 $= 0.20 \text{ MVar}$
Thus for $V_{S} = 145 \text{ KV}$, $V_{r} = 132 \text{ KV}$ and $P_{r} = 187 \text{ MW}$,
alagging MVar of 0.2 will be supplied from the line
along with the real gower of 45 MW . Since the load
requires 36 MMar lagging, the static compensation
 $(bo Find)$
 $(or must ab surb 35.8 MVar leading). The capacity of reatice
 $Capacitors$ is, therefore, 35.8 MVar.$

$$|V_{s}| = |V_{r}| = 132 \text{ kV}, \quad Q_{r} = 0$$

$$Q_{r} = |V_{s}||V_{r}||B|^{2} \sin(\beta - \delta) - |A||V_{r}|^{2}|B|^{2} \sin(\beta - \kappa)$$

$$= \frac{(132)(132)}{(100)} \sin(\beta - \delta) - \frac{(0.98)(132)^{2}}{(100)} \sin(75 - \delta)$$

$$= 68.75$$

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$$P_{r} = |V_{s}||V_{r}||B| \cos(\beta - \delta) - |A||V_{r}|^{2}|B|^{2}\cos(\beta - \alpha)$$

$$= \frac{(132)(132)[(0)(68.75)]}{(100)} - \frac{(0.98)(132)}{(100)} \cos(32^{\circ})$$

$$= 63.13 - 52.77$$

= 10.36 MW

» The development at simple distribution system [open-loop] Network arrangements

When a consumer requests electrical power from a supply authority, ideally all that is required is a cable and a transformer, shown physically as in Figure below. T2 Consumer2

Consumer 1 Ti Power T3 Consumer3

A simple distribution system

Advantages If a fault occurs at T2 then only the protection on one leg connecting T2 is called into operation to isolate this leg. The other consumer are not affected.

Disadvantages If the conductor to T2 fails, then supply to this particular consume is lost completely and cannot be restored until the conductor is replaced / repaired. De Radial distribution system with parallel feeders (open loop) This disadvantage (radial) can be overcome by interoducing addit (parallel) feeders (as shown below) connecting each of the consumers radially. However, this requires more cabling and is not always economical.



Radial distribution system with parallel feeders

(Ring main distribution system (closed loop)

The Ring main system, which is the most favored. Here each consumer has two feeders but connected in different paths to ensure continuity of power, in case of conductor failure in any section.



<u>Advantages</u>: Essentially, meets therequirements of two alternative feeds to give loo?, continuity of supply, whilst saving in cabling compared to parallel feeds. Disadvantages;

For faults at Ti fault current is fed into fault via two parallel paths effectively reducing the impedance from the source to the fault location, and hence the fault current is much higher compared to a nachial path. The fault current in particular could vary depending on the exact location of the fault. Protection must therefore be Past and discriminate correctly. so that other consumers are not interrupted.

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1 Inter connected, Network system

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J = 1 = 1
Power Flow Analysis Load Flow Analysis



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Power Flow Study:-

- · Static Analysis at power Network
- · Real power balance (ZPg: ZPDj Ploss)
- · Reactive power balance (E Qgi E Qpj Qloss)
- · Transmission Flow Limit.
- · Bus Voltage Limits.

Static Analysis & power Network
Mathematical Model of the Network.
Transmission Line - nominal Trodel.
Bus power injections -Sk = VkIk = Pk + jQk

$$P_k = P_{Gk} - P_{Lk}$$
.

» Formation of Bus Admittance Matrix



6

$$\begin{aligned} I_{1} &= \mathcal{Y}_{120} V_{1} + \mathcal{Y}_{12} \left(V_{1} - V_{2} \right) + \mathcal{Y}_{130} V_{1} + \mathcal{Y}_{13} \left(V_{1} - V_{3} \right) \\ I_{2} &= \mathcal{Y}_{210} V_{2} + \mathcal{Y}_{12} \left(V_{2} - V_{1} \right) + \mathcal{Y}_{130} V_{2} + \mathcal{Y}_{23} \left(V_{2} - V_{3} \right) \\ I_{3} &= \mathcal{Y}_{310} V_{3} + \mathcal{Y}_{13} \left(V_{3} - V_{1} \right) + \mathcal{Y}_{320} V_{3} + \mathcal{Y}_{23} \left(V_{3} - V_{2} \right) \\ \begin{bmatrix} I_{1} \\ I_{3} \\ I_{3} \end{bmatrix} &= \begin{bmatrix} \left(\mathcal{Y}_{11} + \mathcal{Y}_{12} + \mathcal{Y}_{133} + \mathcal{Y}_{13} \right) - \mathcal{Y}_{1} - \mathcal{Y}_{13} \\ - \mathcal{Y}_{11} \left(\mathcal{Y}_{11} + \mathcal{Y}_{12} + \mathcal{Y}_{13} \right) - \mathcal{Y}_{1} \\ \mathcal{Y}_{11} \end{bmatrix} \begin{bmatrix} V_{1} \\ Y_{21} & Y_{22} & Y_{13} \\ Y_{31} & -\mathcal{Y}_{32} & \mathcal{Y}_{33} \end{bmatrix} \begin{bmatrix} V_{1} \\ V_{2} \\ V_{3} \end{bmatrix} \\ \mathcal{Y}_{11} &= \mathcal{Y}_{10} + \mathcal{Y}_{12} + \mathcal{Y}_{12} & Y_{13} \\ \mathcal{Y}_{11} &= \mathcal{Y}_{10} + \mathcal{Y}_{12} + \mathcal{Y}_{120} + \mathcal{Y}_{12} \\ \mathcal{Y}_{33} &= \mathcal{Y}_{310} + \mathcal{Y}_{12} + \mathcal{Y}_{120} + \mathcal{Y}_{12} \\ \mathcal{Y}_{33} &= \mathcal{Y}_{310} + \mathcal{Y}_{12} + \mathcal{Y}_{120} + \mathcal{Y}_{12} \\ \mathcal{Y}_{12} &= \mathcal{Y}_{21} = -\mathcal{Y}_{12} \\ \mathcal{Y}_{12} &= \mathcal{Y}_{21} = -\mathcal{Y}_{12} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{31} = -\mathcal{Y}_{13} \\ \mathcal{Y}_{12} &= \mathcal{Y}_{32} = -\mathcal{Y}_{13} \\ \mathcal{Y}_{12} &= \mathcal{Y}_{32} = -\mathcal{Y}_{13} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{13} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{13} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{23} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{23} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = \mathcal{Y}_{32} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{32} = -\mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{33} = \mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{33} = \mathcal{Y}_{33} \\ \mathcal{Y}_{13} &= \mathcal{Y}_{33} \\ \mathcal{Y}_{13} \\$$

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(7)

Characteristics at Yous Matrix:

- Dimension at Yous is (NXN) → N = Number at buses.
- · Ybus is symmetric matrix
- Nous is a sparse matrix (up to 90% to 95% sparse)
- elements Incident to bus :«
- Off-diagonal Elements Yij = Yji are obtained as negative ad admittance Connecting bus i and j

Pawer Flow Equations 8- $I_{k} = \sum_{n=1}^{N} \left(\# cd^{2} busc)^{1} \right) \left(\prod_{i=1}^{I_{1}} = \begin{bmatrix} Y_{11} & Y_{12} & Y_{13} \\ Y_{21} & Y_{22} & Y_{23} \\ Y_{31} & Y_{32} & Y_{33} \end{bmatrix} \begin{bmatrix} Y_{1} \\ Y_{2} \\ Y_{3} \end{bmatrix} \left(Y_{31} & Y_{32} & Y_{33} \end{bmatrix} \begin{bmatrix} Y_{1} \\ Y_{2} \\ Y_{3} \end{bmatrix} \left(Y_{31} & Y_{32} & Y_{33} \end{bmatrix} \left(Y_{31} \right)$ I BUS = YBUS VBUS N (# col bruce) $S_{k} = P_{k} + j Q_{k} = V_{k} I_{k}$ $G_{msk} = V_{k} \left[\sum_{n=1}^{N} Y_{kn} V_{n} \right]^{*} \quad k = 1, 2, 3, ..., N$ $P_{k} + j Q_{k} = V_{k} \left[\sum_{n=1}^{N} Y_{kn} V_{n} \right]^{*} \quad k = 1, 2, 3, ..., N$ $V_n = V_n e^{j\theta_{kn}} angle d tre admittance}$ $Y_{kn} = Y_{kn} e^{j\theta_{kn}} K, n = 1, 2,$ $K,n = 1, 2, 3, \dots, N$ $P_{k} + jQ_{k} = V_{k} \sum_{n=1}^{N} Y_{kn} V_{n} e^{j(\delta_{k} - \delta_{kn} - \Theta_{kn})}$ $P_{k} = V_{k} \sum_{n=1}^{N} Y_{kn} V_{n} \cos \left(\delta_{k} - \delta_{n} - \Theta_{kn} \right)$ $Q_{k} = V_{k} \sum_{n-1}^{N} Y_{kn} V_{n} \sin(\delta k - \delta_{n} - \Theta_{kn})$ 2+ K=+-The admittance + lat connected bus k to all other Characteristics. of Power Flow Equations & * Power Flow Equations are Algebraic ((There is no driffatine or driffations)) - Static System. because we * Power Flow Equations are Mon-linear (Sin, Cos) - Iterative Solution (and multiplication) * Relate P, Q in teams at N, S and YBUS Elements $-P, Q \rightarrow F(v, \delta)$

Characterization & Variables: - (42) System having * Load (PL, QL) = Unranhallal (n. 1) * Load (PL, QL) -> Uncontrolled (Disturbance) Variable. Economiet & Generation (PG, QG) => Control Variable. ((depends on the Long)) Long) * Voltage (V, 8) => State Variable. For a Given Operating Condiction -> Loads and Generations at all buses are known (Specified) => Find the Voltage Magnitude and Angle (V18) at each bus. The states spin and o blem in Yover Flow -> All generation Variables (PG, QG) can not be specified as Losses are not known a priori. Ghoose one bus as reference where Voltage Magnitud and angle are specified. The losses are assigned to this bus. This bus is called "Slack Bus". Classification of Busbars 3bus lypes :-I Swing Bus - There is only one swing bus, (Gold Gues) Une swing bus, which for <u>convenience</u> is numbered bus 1. The swing bus is a reference bus for which V, 1Si, typically 1.0 Lo° per unit, is specified (input data). The num Pl The power-flow program computer frand Q.

E Load bus - Pk and Qk are specified (input data). The power flow program computer Vk and Sk. Voltage Controlled bus - Pk and Vk are input data. 3 The power flow program computes Qk and bk. Examples are buses which generators, switched shunt capacitor, or static var system are connected. Maximum and minimum var Limits QGK, max, QGK, min that this equipment can supply are also input data. Another Examplei is a bus to which a tap changing transformer is connected; in provident a tap changing transformer s-j--i-rije

6.4 POWER FLOW SOLUTION

Power flow studies, commonly known as *load flow*, form an important part of power system analysis. They are necessary for planning, economic scheduling, and control of an existing system as well as planning its future expansion. The problem consists of determining the magnitudes and phase angle of voltages at each bus and active and reactive power flow in each line.

In solving a power flow problem, the system is assumed to be operating under balanced conditions and a single-phase model is used. Four quantities are associated with each bus. These are voltage magnitude |V|, phase angle δ , real power P, and reactive power Q. The system buses are generally classified into three types.

- Slack bus One bus, known as *slack* or *swing bus*, is taken as reference where the magnitude and phase angle of the voltage are specified. This bus makes up the difference between the scheduled loads and generated power that are caused by the losses in the network.
- Load buses At these buses the active and reactive powers are specified. The magnitude and the phase angle of the bus voltages are unknown. These buses are called P-Q buses.
- Regulated buses These buses are the generator buses. They are also known as *voltage-controlled buses*. At these buses, the real power and voltage magnitude are specified. The phase angles of the voltages and the reactive power are to be determined. The limits on the value of the reactive power are also specified. These buses are called P-V buses.

6.4.1 POWER FLOW EQUATION

Consider a typical bus of a power system network as shown in Figure 6.7. Transmission lines are represented by their equivalent π models where impedances have been converted to per unit admittances on a common MVA base.

Application of KCL to this bus results in

$$I_{i} = y_{i0}V_{i} + y_{i1}(V_{i} - V_{1}) + y_{i2}(V_{i} - V_{2}) + \dots + y_{in}(V_{i} - V_{n})$$

= $(y_{i0} + y_{i1} + y_{i2} + \dots + y_{in})V_{i} - y_{i1}V_{1} - y_{i2}V_{2} - \dots - y_{in}V_{n}$ (6.23)

Constitution af Busbars :-

1. Swing Bus (No S.) 2. PV Bus (Voltage Control Bus)

3. PQ Bus (Load Bus)

With each bus i, 4 variables (Pi, Qi, Vi, and Si) are associated. Depending on the great bus two variables are specified (known) and two unknown variables are obtained from power flow solution.



Bus Data

Bus	Type	V Per unit	S	PG per unit	Qq per unit	PL per unit	QL per unit	Qquer per unit	Q Gmin per vinit
1	Swing	1.03	0	-	-				
23	1.50	科教师	100			· 1.	in ji	and a	
4	; ; ; -}	1	1	17/2				100	

Power Flow Solution by Gauss-Seidel Method

$$I_{RUS} = Y_{RUS} V_{RUS}$$

$$I_{k} = \sum_{n=1}^{M} Y_{kn} V_{n}$$

$$S_{k} = P_{k} + jQ_{k} = V_{k} I_{k}^{*}$$

$$P_{k} + jQ_{k} = V_{k} \left[\sum_{n=1}^{M} Y_{kn} V_{n} \right]^{*}$$

$$K = 1, 2, \dots, N$$

$$I_{k} = \frac{P_{k} - jQ_{k}}{V_{k}}, \quad plice$$

$$F_{k} + jQ_{k} = V_{k} \left[\frac{P_{k}}{N_{k}} + V_{n} \right]^{*}$$

$$I_{k} = \frac{P_{k} - jQ_{k}}{V_{k}}, \quad plice$$

$$F_{k} - jQ_{k} = V_{k} I_{k}$$

$$I_{k} = \sum_{n=1}^{N} Y_{kn} V_{n}, \text{ or } F_{k} - jQ_{k} = V_{k} I_{k}$$

$$I_{k} = \sum_{n=1}^{N} Y_{kn} V_{n}, \text{ or } F_{k} - jQ_{k} = V_{k} I_{k}$$

$$I_{k} = Y_{k1} V_{1} + Y_{k2} V_{2} + \dots + Y_{kN} V_{k}$$

$$V_{k} = \sum_{n=1}^{T} \sum_{n=1}^{T} \left[Y_{kn} V_{1} + Y_{k2} V_{2} + \dots + Y_{kN} V_{n} \right]$$

$$V_{k} = \sum_{n=1}^{T} \sum_{n=1}^{T} \left[Y_{kn} V_{1} + Y_{k2} V_{2} + \dots + Y_{kN} V_{n} \right]$$

$$V_{k} = \sum_{n=1}^{T} \sum_{n=1}^{T} \sum_{n=1}^{T} \left[Y_{kn} V_{1} + Y_{k2} V_{2} + \dots + Y_{kN} V_{n} \right]$$

$$V_{k} = \sum_{n=1}^{T} \sum_{$$

Continue iteration till I VK - VK I TE Algorithm Steps :-10 With Pgi, Qgi, Pdi, and Qd: Known Calculate bus injections Pi, Qi 3. Set initial voltage Vi, Si 2. Form YBUS Matrix the durite wedet ind y alies 4. Iteratively solve equation $V_{k}^{(4)} = \frac{1}{V_{k}} \left[\frac{P_{k} - jQ_{k}}{V_{k}^{*}} - \left(\frac{\Sigma}{n-1} \frac{V_{kn}}{V_{n}} + \frac{\Sigma}{n-1} \frac{V_{kn}}{N-1} + \frac{\Sigma}{n-1} \frac{V_{kn}}{N-1} \right) \right]$ to obtain new values at bus voltages. Algorithm Modification when PV Buses are also Present $Q_{i} = - I_{m} \left[V_{i}^{*} \sum_{k=1}^{k} Y_{ik} V_{k} \right] \qquad P_{k} + j Q_{k} = V_{k} I_{k} D_{k}^{*}$ $Q_{k} = - I_{m} \left[V_{i}^{*} \sum_{k=1}^{k} Y_{ik} V_{k} \right] \qquad Q_{k} = - I_{m} \left[V_{k}^{*} I_{k} \right]$ Qk = - Im[Vk Ik] $Q_{i}^{(r+1)} = -\operatorname{Im}\left[\left(V_{i}^{(r)}\right)^{*} \sum_{k=1}^{i'} Y_{ik} V_{k}^{(r+1)} + \left(V_{i}^{(r)}\right)^{*} \sum_{i=1}^{r} U_{ik} V_{k}^{(r)}\right]$ The revessed value of Si is obtained from immediately following $S_{i}^{(r+1)} = \begin{bmatrix} V_{i}^{(r+1)} \\ V_{i}^{(r+1)} \end{bmatrix}$ step1 . Thus = Angle at $\left[\frac{A_{i}^{(n+1)}}{(V_{i}^{(n)})^{*}} - \frac{\sum_{k=1}^{i-1}}{B_{ik}} \frac{V_{k}^{(n+1)}}{k} - \frac{\sum_{k=1}^{n}}{B_{ik}} \frac{V_{k}}{k}\right]$ Where A(++1) = Pi - j Qi The algorithm for PQ buses remains unchanged.

Example ? For the system shown,
$$Z_{1} = j \cdot 5 \cdot V_{1} = 1 \cdot 6^{\circ}$$

 $S_{g_{2}} = j \cdot 0$ and $S_{02} = 0.5 + j \cdot 0 \cdot 5$ Find V_{2} using
Gauss-Seidel iteration technique.
 $V_{1} = 1 + j^{\circ}$
 $V_{1} = -j^{\circ}$
 $V_{2} = -j^{\circ}$
 $V_{1} = 1 - j^{\circ}$
 $S_{2} = S_{02} - S_{02} = -0.5$
 P_{1} thing the values of $V_{1} \cdot J_{2} \cdot J_{21}$ and V_{1} in
equation (1), we get
 $V_{1}^{\circ} = -j [0.25/(V_{2})^{\circ}] + 1.0 = ---$

Short with a quess, taking
$$V_1 = 1$$
 L° and iterate using equation (2).
We have, $V_2 = 1 + j^{\circ}$
Putting in equation (2), and iterating for V_2 , we get
 $V_2 = -j [0.25](1+jo)^{\dagger}] + 1.0$
 $= 1.0 - j 0.25$
 $V_1 = 1.0307 + 6 [-141.0362243^{\circ}]$
 $V_2 = -j [0.25](1.0 - j 0.25)^{\dagger}] + 1.0$
 $= 1.0 - j 0.25 [(1.0 + j 0.25)^{\dagger}] + 1.0$
 $= 1.0 [(1.0 + j 0.25)]$
 $= 0.9 = 0.9 = 0.143 [-141.036249^{\circ}]$

Similarly, we can iterate it further. The results of the iteration, are tabulated below V_1 V_2 V_1 V_2 V_3 V_4 V_2 V_4 V_2 V_4 V_2 V_4 V_2 V_4 V_2 V_4 V_2 V_4 V_4 V_2 V_4 V_4 V_2 V_4 V_4

1	Iberation #	V2
1	0	$1 \lfloor 0 \end{pmatrix} \Rightarrow$
0.030776		1.030776 -14.036243
0.060633	2	0.9701432-14.0362490
0,000/18	3	0.970261 [-14.931409 =>
0.004026	ų	0.966235 -14.931416 ->>
0.000001	5	0.966236 -14.995078
0.000756	6	0.965948 - 14.9950720

Since, the difference in the values for the voltage doesn't change much between the 5th and 6th iteration, we can stop at the 6th. Hence, we can see that starting with the value yillo, convergence is reached in site stops. (B)



unit. The scheduled loads at buses 2 and 3 are as marked on the diagram. Line impedances are marked in per unit on a 100-MVA base and the line charging susceptances are neglected.



FIGURE 6.9

One-line diagram of Example 6.7 (impedances in pu on 100-MVA base).

(a) Using the Gauss-Seidel method, determine the phasor values of the voltage at the load buses 2 and 3 (P-Q buses) accurate to four decimal places.

(b) Find the slack bus real and reactive power.

(c) Determine the line flows and line losses. Construct a power flow diagram showing the direction of line flow.

(a) Line impedances are converted to admittances

$$y_{12} = \frac{1}{0.02 + j0.04} = 10 - j20$$

Similarly, $y_{13} = 10 - j30$ and $y_{23} = 16 - j32$. The admittances are marked on the network shown in Figure 6.10.

At the P-Q buses, the complex loads expressed in per units are

$$S_2^{sch} = -\frac{(256.6 + j110.2)}{100} = -2.566 - j1.102 \text{ pu}$$
$$S_3^{sch} = -\frac{(138.6 + j45.2)}{100} = -1.386 - j0.452 \text{ pu}$$

Since the actual admittances are readily available in Figure 6.10, for hand calculation, we use (6.28). Bus 1 is taken as reference bus (slack bus). Starting from an initial estimate of $V_2^{(0)} = 1.0 + j0.0$ and $V_3^{(0)} = 1.0 + j0.0$, V_2 and V_3 are computed from (6.28) as follows

$$V_2^{(1)} = \frac{\frac{P_2^{sch} - jQ_2^{sch}}{V_2^{*(0)}} + y_{12}V_1 + y_{23}V_3^{(0)}}{y_{12} + y_{23}}$$

$$V_{k}^{(+1)} = \frac{1}{Y_{kk}} \left[\frac{P_{k} - jQ_{k}}{V_{k}^{+(i)}} - \left(\sum_{n=1}^{k-1} Y_{kn} V_{n}^{(+1)} + \sum_{n=k+1}^{k} Y_{kn} V_{n}^{(-)} \right) \right]$$



FIGURE 6.10

One-line diagram of Example 6.7 (admittances in pu on 100-MVA base).

$$N_{2} = \frac{\frac{-2.566+j1.102}{1.0-j0} + (10-j20)(1.05+j0) + (16-j32)(1.0+j0)}{(26-j52)}$$

= $\underbrace{0.9825 - j0.0310}_{\text{nd}}$ To four decimal places.

and

$$V_{3}^{(1)} = \frac{\frac{P_{3}^{sch} - jQ_{3}^{sch}}{V_{3}^{*(0)}} + y_{13}V_{1} + y_{23}V_{2}^{(1)}}{y_{13} + y_{23}}}{\frac{-1.386 + j0.452}{1 - j0} + (10 - j30)(1.05 + j0) + (16 - j32)(0.9825 - j0.0310)}{(26 - j62)}}$$
$$= 1.0011 - j0.0353$$

For the second iteration we have

$$V_2^{(2)} = \frac{\frac{-2.566+j1.102}{0.9825+j0.0310} + (10-j20)(1.05+j0) + (16-j32)(1.0011-j0.0353)}{(26-j52)}$$

= 0.9816 - i0.0520

and

$$V_{3}^{(2)} = \frac{\frac{-1.386+j0.452}{1.0011+j0.0353} + (10-j30)(1.05+j0) + (16-j32)(0.9816-j0.052)}{(26-j62)}$$

= 1.0008 - j0.0459

The process is continued and a solution is converged with an accuracy of 5×10^{-5} per unit in seven iterations as given below.

$$V_2^{(3)} = 0.9808 - j0.0578$$
 $V_3^{(3)} = 1.0004 - j0.0488$

$V_2^{(4)} = 0.9803 - j0.0594$	$V_3^{(4)} = 1.0002 - j0.0497$
$V_2^{(5)} = 0.9801 - j0.0598$	$V_3^{(5)} = 1.0001 - j0.0499$
$V_2^{(6)} = 0.9801 - j0.0599$	$V_3^{(6)} = 1.0000 - j0.0500$
$V_2^{(7)} = 0.9800 - j0.0600$	$V_3^{(7)} = 1.0000 - j0.0500$

The final solution is

$$V_2 = 0.9800 - j0.0600 = 0.98183 \angle -3.5035^\circ$$
 pu
 $V_3 = 1.0000 - j0.0500 = 1.00125 \angle -2.8624^\circ$ pu

(b) With the knowledge of all bus voltages, the slack bus power is obtained from (6.27)

$$P_1 - jQ_1 = V_1^* [V_1(y_{12} + y_{13}) - (y_{12}V_2 + y_{13}V_3)]$$

= 1.05[1.05(20 - j50) - (10 - j20)(0.98 - j.06) -
(10 - j30)(1.0 - j0.05)]
= 4.095 - j1.890

or the slack bus real and reactive powers are $P_1 = 4.095$ pu = 409.5 MW and $Q_1 = 1.890$ pu = 189 Mvar.

(c) To find the line flows, first the line currents are computed. With line charging capacitors neglected, the line currents are

$$I_{12} = y_{12}(V_1 - V_2) = (10 - j20)[(1.05 + j0) - (0.98 - j0.06)] = 1.9 - j0.8$$

$$I_{21} = -I_{12} = -1.9 + j0.8$$

$$I_{13} = y_{13}(V_1 - V_3) = (10 - j30)[(1.05 + j0) - (1.0 - j0.05)] = 2.0 - j1.0$$

$$I_{31} = -I_{13} = -2.0 + j1.0$$

$$I_{23} = y_{23}(V_2 - V_3) = (16 - j32)[(0.98 - j0.06) - (1 - j0.05)] = -.64 + j.48$$

$$I_{32} = -I_{23} = [0.64 - j0.48]$$

The line flows are

$$\begin{split} S_{12} &= V_1 I_{12}^* = (1.05 + j0.0)(1.9 + j0.8) = 1.995 + j0.84 \text{ pu} \\ &= 199.5 \text{ MW} + j84.0 \text{ Mvar} \\ S_{21} &= V_2 I_{21}^* = (0.98 - j0.06)(-1.9 - j0.8) = -1.91 - j0.67 \text{ pu} \\ &= -191.0 \text{ MW} - j67.0 \text{ Mvar} \\ S_{13} &= V_1 I_{13}^* = (1.05 + j0.0)(2.0 + j1.0) = 2.1 + j1.05 \text{ pu} \\ &= 210.0 \text{ MW} + j105.0 \text{ Mvar} \end{split}$$

$$S_{31} = V_3 I_{31}^* = (1.0 - j0.05)(-2.0 - j1.0) = -2.05 - j0.90 \text{ pu}$$

= -205.0 MW - j90.0 Mvar
$$S_{23} = V_2 I_{23}^* = (0.98 - j0.06)(-0.656 + j0.48) = -0.656 - j0.432 \text{ pu}$$

= -65.6 MW - j43.2 Mvar
$$S_{32} = V_3 I_{32}^* = (1.0 - j0.05)(0.64 + j0.48) = 0.664 + j0.448 \text{ pu}$$

= 66.4 MW + j44.8 Mvar

and the line losses are

 $S_{L\ 12} = S_{12} + S_{21} = 8.5 \text{ MW} + j17.0 \text{ Mvar}$ $S_{L\ 13} = S_{13} + S_{31} = 5.0 \text{ MW} + j15.0 \text{ Mvar}$ $S_{L\ 23} = S_{23} + S_{32} = 0.8 \text{ MW} + j1.60 \text{ Mvar}$

The power flow diagram is shown in Figure 6.11, where real power direction is indicated by \rightarrow and the reactive power direction is indicated by \mapsto . The values within parentheses are the real and reactive losses in the line.



FIGURE 6.11

Power flow diagram of Example 6.7 (powers in MW and Mvar).

Example 6.8 (chp6ex8)

Figure 6.12 shows the one-line diagram of a simple three-bus power system with generators at buses 1 and 3. The magnitude of voltage at bus 1 is adjusted to 1.05 pu. Voltage magnitude at bus 3 is fixed at 1.04 pu with a real power generation of 200 MW. A load consisting of 400 MW and 250 Mvar is taken from bus 2. Line impedances are marked in per unit on a 100 MVA base, and the line charging susceptances are neglected. Obtain the power flow solution by the Gauss-Seidel method including line flows and line losses.





Line impedances converted to admittances are $y_{12} = 10 - j20$, $y_{13} = 10 - j30^{\circ}$ and $y_{23} = 16 - j32$. The load and generation expressed in per units are

(Load)
$$S_2^{sch} = -\frac{(400 + j250)}{100} = -4.0 - j2.5$$
 pu
(gen.) $P_3^{sch} = \frac{200}{100} = 2.0$ pu

Bus 1 is taken as the reference bus (slack bus). Starting from an initial estimate of $V_2^{(0)} = 1.0 + j0.0$ and $V_3^{(0)} = 1.04 + j0.0$, V_2 and V_3 are computed from (6.28).

$$V_{2}^{(1)} = \frac{\frac{P_{2}^{sch} - jQ_{2}^{sch}}{V_{2}^{*(0)}} + y_{12}V_{1} + y_{23}V_{3}^{(0)}}{y_{12} + y_{23}}$$
$$= \frac{\frac{-4.0 + j2.5}{1.0 - j0} + (10 - j20)(1.05 + j0) + (16 - j32)(1.04 + j0)}{(26 - j52)}$$
$$= 0.97462 - j0.042307$$

Bus 3 is a regulated bus where voltage magnitude and real power are specified. For the voltage-controlled bus, first the reactive power is computed from (6.30)

$$Q_3^{(1)} = -\Im\{V_3^{*^{(0)}}[V_3^{(0)}(y_{13} + y_{23}) - y_{13}V_1 - y_{23}V_2^{(1)}]\}$$

= $-\Im\{(1.04 - j0)[(1.04 + j0)(26 - j62) - (10 - j30)(1.05 + j0) - (16 - j32)(0.97462 - j0.042307)]\}$
= 1.16

$$Q_{i}^{(r+1)} = -\operatorname{Im}\left[\left(V_{i}^{(r)}\right)^{*} \sum_{k=1}^{(r+1)} V_{ik} \frac{(r+1)}{k} + \left(V_{i}^{(r)}\right)^{*} \sum_{k=1}^{n} V_{ik} \frac{(r+1)}{k}\right]$$

$$Q_{i}^{(r)} = -\operatorname{Im}\left[V_{i}^{*} \sum_{k=1}^{n} V_{ik} \frac{(r+1)}{k}\right]$$

$$\frac{Q_{i}^{(r)}}{k} = -\operatorname{Im}\left[V_{i}^{*} \sum_{k=1}^{n} V_{ik} \frac{(r+1)}{k}\right]$$

The value of $Q_3^{(1)}$ is used as Q_3^{sch} for the computation of voltage at bus 3. The complex voltage at bus 3, denoted by $V_{c3}^{(1)}$, is calculated

$$V_{c3}^{(1)} = \frac{\frac{P_{3}^{sch} - jQ_{3}^{sch}}{V_{3}^{(0)}} + y_{13}V_{1} + y_{23}V_{2}^{(1)}}{y_{13} + y_{23}}$$

$$= \frac{\frac{2.0 - j1.16}{1.04 - j0} + (10 - j30)(1.05 + j0) + (16 - j32)(0.97462 - j0.042307)}{(26 - j62)}$$

$$= 1.03783 - j0.005170$$

Since $|V_3|$ is held constant at 1.04 pu, only the imaginary part of $V_{c3}^{(1)}$ is retained, i.e, $f_3^{(1)} = -0.005170$, and its real part is obtained from real part = $e_3^{(1)} = \sqrt{(1.04)^2 - (0.005170)^2} = 1.039987$ Thus Thus

rcal part =
$$e_3^{(1)} = \sqrt{(1.04)^2 - (0.005170)^2} = 1.039987$$

$$V_3^{(1)} = 1.039987 - j0.005170$$

For the second iteration, we have

$$V_{2}^{(2)} = \frac{\frac{P_{2}^{sch} - jQ_{2}^{sch}}{V_{2}^{*(1)}} + y_{12}V_{1} + y_{23}V_{3}^{(1)}}{y_{12} + y_{23}}$$
$$= \frac{\frac{-4.0 + j2.5}{.97462 + j.042307} + (10 - j20)(1.05) + (16 - j32)(1.039987 + j0.005170)}{(26 - j52)}$$
$$= 0.971057 - j0.043432$$

$$Q_{3}^{(2)} = -\Im\{V_{3}^{*^{(1)}}[V_{3}^{(1)}(y_{13} + y_{23}) - y_{13}V_{1} - y_{23}V_{2}^{(2)}]\}$$

= $-\Im\{(1.039987 + j0.005170)[(1.039987 - j0.005170)(26 - j62) - (10 - j30)(1.05 + j0) - (16 - j32)(0.971057 - j0.043432)]\}$
= 1.38796

$$V_{c3}^{(2)} = \frac{\frac{P_3^{sch} - jQ_3^{sch}}{V_3^{*(1)}} + y_{13}V_1 + y_{23}V_2^{(2)}}{y_{13} + y_{23}}$$

= $\frac{\frac{2.0 - j1.38796}{1.039987 + j0.00517} + (10 - j30)(1.05) + (16 - j32)(.971057 - j.043432)}{(26 - j62)}$
= $1.03908 - j0.00730$

Since $|V_3|$ is held constant at 1.04 pu, only the imaginary part of $V_{c3}^{(2)}$ is retained, i.e., $f_3^{(2)} = -0.00730$, and its real part is obtained from

$$e_3^{(2)} = \sqrt{(1.04)^2 - (0.00730)^2} = 1.039974$$

or

 $V_3^{(2)} = 1.039974 - j0.00730$

The process is continued and a solution is converged with an accuracy of 5×10^{-5} pu in seven iterations as given below.

$V_2^{(3)} = 0.97073 - j0.04479$	$Q_3^{(3)} = 1.42904$	$V_3^{(3)} = 1.03996 - j0.00833$
$V_2^{(4)} = 0.97065 - j0.04533$	$Q_3^{(4)} = 1.44833$	$V_3^{(4)} = 1.03996 - j0.00873$
$V_2^{(5)} = 0.97062 - j0.04555$	$Q_3^{(5)} = 1.45621$	$V_3^{(5)} = 1.03996 - j0.00893$
$V_2^{(6)} = 0.97061 - j0.04565$	$Q_3^{(6)} = 1.45947$	$V_3^{(6)} = 1.03996 - j0.00900$
$V_2^{(7)} = 0.97061 - j0.04569$	$Q_3^{(7)} = 1.46082$	$V_3^{(7)} = 1.03996 - j0.00903$
The final solution is		

 $V_2 = 0.97168 \angle -2.6948^\circ$ pu

 $S_3 = 2.0 + j1.4617$ pu $V_3 = 1.04 \angle -.498^\circ$ pu $S_1 = 2.1842 + j1.4085$ pu

Line flows and line losses are computed as in Example 6.7, and the results expressed in MW and Mvar are

$$\begin{split} S_{12} &= 179.36 + j118.734 \quad S_{21} = -170.97 - j101.947 \quad S_{L\,12} = 8.39 + j16.79 \\ S_{13} &= 39.06 + j22.118 \quad S_{31} = -38.88 - j\,21.569 \quad S_{L\,13} = 0.18 + j0.548 \\ S_{23} &= -229.03 - j148.05 \quad S_{32} = 238.88 + j167.746 \quad S_{L\,23} = 9.85 + j19.69 \end{split}$$

The power flow diagram is shown in Figure 6.13, where real power direction is indicated by \rightarrow and the reactive power direction is indicated by \rightarrow . The values within parentheses are the real and reactive losses in the line.

 $P_{1} - jQ_{1} = V_{1}^{*} \left[V_{1} \left(y_{12} + y_{13} \right) - \left(y_{12} + y_{13} + y_{13} \right) \right]$

* for slack bus



FIGURE 6.13 Power flow diagram of Example 6.8 (powers in MW and Mvar).

6.7 TAP CHANGING TRANSFORMERS

In Section 2.6 it was shown that the flow of real power along a transmission line is determined by the angle difference of the terminal voltages, and the flow of reactive power is determined mainly by the magnitude difference of terminal voltages. Real and reactive powers can be controlled by use of tap changing transformers and regulating transformers.

In a tap changing transformer, when the ratio is at the nominal value, the transformer is represented by a series admittance y_t in per unit. With off-nominal ratio, the per unit admittance is different from both sides of the transformer, and the admittance must be modified to include the effect of the off-nominal ratio. Consider a transformer with admittance y_t in series with an ideal transformer representing the off-nominal tap ratio 1:*a* as shown in Figure 6.14. y_t is the admittance in per unit based on the nominal turn ratio and *a* is the per unit off-nominal tap position allowing for small adjustment in voltage of usually ± 10 percent. In the case of phase shifting transformers, *a* is a complex number. Consider a fictitious bus *x* between the turn ratio and admittance of the transformer. Since the complex power on either side of the ideal transformer is the same, it follows that if the voltage goes through a positive phase angle shift, the current will go through a negative phase angle shift. Thus, for the assumed direction of currents, we have

$$V_x = \frac{1}{a}V_j \tag{6.43}$$

$$I_i = -a^* I_j \tag{6.44}$$

The current I_i is given by

 $I_i = y_t (V_i - V_x)$

Balanced and Unbalanced Faults

Fault Analysis

- » An essential part of a power network is the Calculation of the currents which flow in the components when faults of various types occur.
 - » In a fault survey, faults are applied at various points in the network and the resulting currents obtained by hand Calculation, or, most likely now on large networks, by computer softwares
- » The magnitude of the fault currents give the engineer the current settings for the protection to be used and the ratings of the circuit breakers

» Types at Short Circuit:

Line-Line faut L-L

Zr 70-89% 5-7% 10-12% S-10%

Asymmetrical Faults Unbalanced Faults

Symmetrical Faults Balanced Faults

if Zf = 0 ⇒ Solid Fault, Bolted Fault

» The most common of these faults is the short circuit of a single phase to ground fault. » Often the path to ground contains resistance in the form I an are as shown in the previous figure. » Although the single line to ground fault is the most common, calculations are frequently performed to 30 faults. » 30 faults (Balanced faults) are the most severe fault and easy to calculate. » The problem consists of determining bus voltages and line currents during various types out faults.

9.2 BALANCED THREE-PHASE FAULT

This type of fault is defined as the simultaneous short circuit across all three phases. It occurs infrequently, but it is the most severe type of fault encountered. Because the network is balanced, it is solved on a per-phase basis. The other two phases carry identical currents except for the phase shift.

the reactance of the synchronous generator under short-circuit conditions is a time-varying quantity, and for network analysis three reactances were defined. The subtransient reactance X''_d , for the first few cycles of the short circuit current, transient reactance X'_d , for the next (say) 30 cycles, and the synchronous reactance X_d , thereafter. Since the duration of the short circuit current depends on the time of operation of the protective system, it is not always easy to decide which reactance to use. Generally, the subtransient reactance is used for determining the interrupting capacity of the circuit breakers. In fault studies required for relay setting and coordination, transient reactance is used. Also, in typical transient stability studies, transient reactance is used.

A fault represents a structural network change equivalent with that caused by the addition of an impedance at the place of fault. If the fault impedance is zero, the fault is referred to as the *bolted fault* or the *solid fault*. The faulted network can be solved conveniently by the Thévenin's method. The procedure is demonstrated in the following example.

Example 9.1 (chp9ex1)

The one-line diagram of a simple three-bus power system is shown in Figure 9.1. Each generator is represented by an emf behind the transient reactance. All impedances are expressed in per unit on a common 100 MVA base, and for simplicity, resistances are neglected. The following assumptions are made.

(i) Shunt capacitances are neglected and the system is considered on no-load.

(*ii*) All generators are running at their rated voltage and rated frequency with their emfs in phase.

Determine the fault current, the bus voltages, and the line currents during the fault when a balanced three-phase fault with a fault impedance $Z_f = 0.16$ per unit occurs on





The fault is simulated by switching on an impedance Z_f at bus 3 as shown in Figure 9.2(a). Thévenin's theorem states that the changes in the network voltage caused by the added branch (the fault impedance) shown in Figure 9.2(a) is equivalent to those caused by the added voltage $V_3(0)$ with all other sources shortcircuited as shown in Figure 9.2(b).



FIGURE 9.2

(a) The impedance network for fault at bus 3. (b) Thévenin's equivalent network.

(a) From 9.2(b), the fault current at bus 3 is

$$I_3(F) = \frac{V_3(0)}{Z_{33} + Z_f}$$

where $V_3(0)$ is the Thévenin's voltage or the prefault bus voltage. The prefault bus voltage can be obtained from the results of the power flow solution. In this example, since the loads are neglected and generator's emfs are assumed equal to the rated value, all the prefault bus voltages are equal to 1.0 per unit, i.e.,

$$V_1(0) = V_2(0) = V_3(0) = 1.0$$
 pu

 Z_{33} is the Thévenin's impedance viewed from the faulted bus.

To find the Thévenin's impedance, we convert the Δ formed by buses 123 to an equivalent Y as shown in Figure 9.3(a).



FIGURE 9.3 Reduction of Thévenin's equivalent network.

$$Z_{1s} = Z_{2s} = \frac{(j0.4)(j0.8)}{j1.6} = j0.2 \qquad Z_{3s} = \frac{(j0.4)(j0.4)}{j1.6} = j0.1$$

Combining the parallel branches, Thévenin's impedance is

$$Z_{33} = \frac{(j0.4)(j0.6)}{j0.4 + j0.6} + j0.1$$

= j0.24 + j0.1 = j0.34

From Figure 9.3(c), the fault current is

()
$$I_3(F) = \frac{V_3(0)}{Z_{33} + Z_f} = \frac{1.0}{j0.34 + j0.16} = -j2.0$$
 pu

With reference to Figure 9.3(a), the current divisions between the two generators are

2)
$$I_{G1} = \frac{j0.6}{j0.4 + j0.6} I_3(F) = -j1.2 \text{ pu}$$
$$I_{G2} = \frac{j0.4}{j0.4 + j0.6} I_3(F) = -j0.8 \text{ pu}$$

For the bus voltage changes from Figure 9.3(b), we get

3)

$$\Delta V_1 = 0 - (j0.2)(-j1.2) = -0.24 \text{ pu}$$

$$\Delta V_2 = 0 - (j0.4)(-j0.8) = -0.32 \text{ pu}$$

$$\Delta V_3 = (j0.16)(-j2) - 1.0 = -0.68 \text{ pu}$$

★ The bus voltages during the fault are obtained by superposition of the prefault bus voltages and the changes in the bus voltages caused by the equivalent emf connected to the faulted bus, as shown in Figure 9.2(b), i.e.,

$$V_1(F) = V_1(0) + \Delta V_1 = 1.0 - 0.24 = 0.76$$
 pu
 $V_2(F) = V_2(0) + \Delta V_2 = 1.0 - 0.32 = 0.68$ pu
 $V_3(F) = V_3(0) + \Delta V_3 = 1.0 - 0.68 = 0.32$ pu

The short circuit-currents in the lines are

$$I_{12}(F) = \frac{V_1(F) - V_2(F)}{z_{12}} = \frac{0.76 - 0.68}{j0.8} = -j0.1 \text{ pu}$$
$$I_{13}(F) = \frac{V_1(F) - V_3(F)}{z_{13}} = \frac{0.76 - 0.32}{j0.4} = -j1.1 \text{ pu}$$
$$I_{23}(F) = \frac{V_2(F) - V_3(F)}{z_{23}} = \frac{0.68 - 0.32}{j0.4} = -j0.9 \text{ pu}$$

(b) The fault with impedance Z_f at bus 2 is depicted in Figure 9.4(a), and its Thévenin's equivalent circuit is shown in Figure 9.4(b). To find the Thévenin's impedance, we combine the parallel branches in Figure 9.4(b). Also, combining parallel branches from ground to bus 2 in Figure 9.5(a), results in

$$Z_{22} = \frac{(j0.6)(j0.4)}{j0.6 + j0.4} = j0.24$$

From Figure 9.5(b), the fault current is

$$I_2(F) = \frac{V_2(0)}{Z_{22} + Z_f} = \frac{1.0}{j0.24 + j0.16} = -j2.5$$
 pu





(a) The impedance network for fault at bus 2. (b) Thévenin's equivalent network.



FIGURE 9.5 Reduction of Thévenin's equivalent network.

With reference to Figure 9.5(a), the current divisions between the generators are

$$I_{G1} = \frac{j0.4}{j0.4 + j0.6} I_2(F) = -j1.0 \text{ pu}$$
$$I_{G2} = \frac{j0.6}{j0.4 + j0.6} I_2(F) = -j1.5 \text{ pu}$$

For the bus voltage changes from Figure 9.4(a), we get

$$\Delta V_1 = 0 - (j0.2)(-j1.0) = -0.2 \text{ pu}$$

$$\Delta V_2 = 0 - (j0.4)(-j1.5) = -0.6 \text{ pu}$$

$$\Delta V_3 = -0.2 - (j0.4)(\frac{-j1.0}{2}) = -0.4 \text{ pu}$$

The bus voltages during the fault are obtained by superposition of the prefault bus voltages and the changes in the bus voltages caused by the equivalent emf connected to the faulted bus, as shown in Figure 9.4(b), i.e.,

$$V_1(F) = V_1(0) + \Delta V_1 = 1.0 - 0.2 = 0.8$$
 pu
 $V_2(F) = V_2(0) + \Delta V_2 = 1.0 - 0.6 = 0.4$ pu
 $V_3(F) = V_3(0) + \Delta V_3 = 1.0 - 0.4 = 0.6$ pu

The short circuit-currents in the lines are

$$I_{12}(F) = \frac{V_1(F) - V_2(F)}{z_{12}} = \frac{0.8 - 0.4}{j0.8} = -j0.5 \text{ pu}$$
$$I_{13}(F) = \frac{V_1(F) - V_3(F)}{z_{13}} = \frac{0.8 - 0.6}{j0.4} = -j0.5 \text{ pu}$$
$$I_{32}(F) = \frac{V_3(F) - V_3(F)}{z_{32}} = \frac{0.6 - 0.4}{j0.4} = -j0.5 \text{ pu}$$

(c) The fault with impedance Z_f at bus 1 is depicted in Figure 9.6(a), and its Thévenin's equivalent circuit is shown in Figure 9.6(b).



FIGURE 9.6

(a) The impedance network for fault at bus 1. (b) Theyenin's equivalent network.

To find the Thévenin's impedance, we combine the parallel branches in Figure 9.6(b). Also, combining parallel branches from ground to bus 1 in Figure 9.7(a),







results in

$$Z_{11} = \frac{(j0.2)(j0.8)}{j0.2 + j0.8} = j0.16$$

From Figure 9.7(b), the fault current is

$$I_1(F) = \frac{V_1(0)}{Z_{11} + Z_f} = \frac{1.0}{j0.16 + j0.16} = -j3.125$$
 pu

With reference to Figure 9.7(a), the current divisions between the two generators are

$$I_{G1} = \frac{j0.8}{j0.2 + j0.8} I_2(F) = -j2.50 \text{ pu}$$
$$I_{G2} = \frac{j0.2}{j0.2 + j0.8} I_2(F) = -j0.625 \text{ pu}$$

For the bus voltage changes from Figure 9.6(b), we get

$$\Delta V_1 = 0 - (j0.2)(-j2.5) = -0.50 \text{ pu}$$

$$\Delta V_2 = 0 - (j0.4)(-j0.625) = -0.25 \text{ pu}$$

$$\Delta V_3 = -0.5 + (j0.4)(\frac{-j0.625}{2}) = -0.375 \text{ pu}$$

Bus voltages during the fault are obtained by superposition of the prefault bus voltages and the changes in the bus voltages caused by the equivalent emf connected to the faulted bus, as shown in Figure 9.6(b), i.e.,

$$V_1(F) = V_1(0) + \Delta V_1 = 1.0 - 0.50 = 0.50$$
 pu
 $V_2(F) = V_2(0) + \Delta V_2 = 1.0 - 0.25 = 0.75$ pu
 $V_3(F) = V_3(0) + \Delta V_3 = 1.0 - 0.375 = 0.625$ pu

The short-circuit currents in the lines are

$$I_{21}(F) = \frac{V_2(F) - V_1(F)}{z_{21}} = \frac{0.75 - 0.5}{j0.8} = -j0.3125 \text{ pu}$$

$$I_{31}(F) = \frac{V_3(F) - V_1(F)}{z_{31}} = \frac{0.625 - 0.5}{j0.4} = -j0.3125 \text{ pu}$$

$$I_{23}(F) = \frac{V_2(F) - V_3(F)}{z_{23}} = \frac{0.75 - 0.625}{j0.4} = -j0.3125 \text{ pu}$$

Notes :-

1) In the above example the load currents were neglected and all prefault bus voltages were assumed to be equal to 1.0 per unit. For more accurate calculation, the prefault bus voltages can be obtained from the power flow solution. As we have seen in Chapter 6, in a power system, loads are specified and the load currents are unknown. One way to include the effects of load currents in the fault analysis is to express the loads by a constant impedance evaluated at the prefault bus voltages. This is a very good approximation which results in linear nodal equations. The procedure is summarized in the following steps.

- The prefault bus voltages are obtained from the results of the power flow solution.
- In order to preserve the linearity feature of the network, loads are converted to constant admittances using the prefault bus voltages.
- The faulted network is reduced into a Thévenin's equivalent circuit as viewed from the faulted bus. Applying Thévenin's theorem, changes in the bus voltages are obtained.
- Bus voltages during the fault are obtained by superposition of the prefault bus voltages and the changes in the bus voltages computed in the previous step.
- The currents during the fault in all branches of the network are then obtained.

Shot Circuit Copacity (SCC):
The Sice at a bus is a common measure of the strength of a bus.
The Sice or the short-circuit MVA at bus K is defined as the
product of the magnitude of the rated bus voltage and the
Pault Current.
Sice = U3 VLK
$$I_K(F) \neq 10^3$$
 MVA
Ly the Cine-to-line voltage expressed in KV
But
 $I_K(F) = I_K(F) p_N + I_B$ base MVA
 $= \frac{I_K(F) p_N}{V_B U^3} \times \frac{S_B + 10^3}{V_B U^3}$ (in KV
 $I_K(F) = \frac{V_K(G)}{X_{KK}} \times \frac{S_B + 10^3}{V_B U^3}$ (in KV
 $I_K(F) = \frac{V_K(G)}{Z_{KK} + \frac{S_B + 10}{V_B U^3}}$ (in KV
 $I_K(F) = \frac{V_K(G)}{Z_{KK} + \frac{S_B + 10}{V_B U^3}}$ (in KV
 $V_K(F) = \frac{V_K(G)}{Z_{KK} + \frac{S_B + 10}{V_B U^3}}$ (in KV
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 $I_K(F) = \frac{V_K(G)}{Z_{KK} + \frac{S_B + 10}{V_B U^3}}$ (in KV)
 $I_K(F) = \frac{S_B - M_{KK}}{M_{KK} + \frac{S_B - M_{KK}}{M_{KK}}}$ (if $V_B = V_{LK}$)
 $I_K(G) = I_{FM}$ (if $S_B - \frac{S_B - M_{KK}}{M_{KK}}$)